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## Research article

# VaR as a mitigating risk tool in the maritime sector: An empirical approach on freight rates 

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## Supplementary

Table 1. Descriptive Statistics.

| Full Sample | 22/5/2007-21/09/2015 |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| In Sample | 22/05/2007-13/08/2013 |  |  |  |  |  |
| Out of Sample | 14/08/2013-21/09/2015 |  |  |  |  |  |
| Route | TC2 Spot | TC2 One month | TC2 Three months | TD3 Spot | TD3 One month | TD3 Three months |
| No of Obs | 2085 | 2085 | 2085 | 2085 | 2085 | 2085 |
| Mean | 158.11 | 158.32 | 154.69 | 63.51 | 62.34 | 60.18 |
| Median | 146.67 | 146.50 | 141.50 | 52.28 | 54.00 | 51.59 |
| Maximum | 386.25 | 353.00 | 305.00 | 319.22 | 215.00 | 180.00 |
| Minimum | 9.55 | 80.00 | 91.00 | 25.36 | 30.00 | 30.50 |
| Std. Dev | 60.10 | 51.57 | 48.43 | 39.68 | 30.84 | 2630 |
| Skewness | 1.33 | 1.21 | 1.23 | 2.92 | 2.31 | 2.02 |
| Kurtosis | 4.99 | 4.03 | 3.57 | 12.85 | 9.04 | 7.67 |
| J-B | 960.70 | 602.42 | 522.88 | 11,394.58 | 5,028.34 | 3,312.13 |

Table 2. Value at Risk Statistics-TC2-Spot price returns.

| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| GARCH (1,1)-N | -8.78\% | -6.21\% | -4.84\% | -60.99\% | -43.13\% | -33.61\% | -7.02\% | -4.96\% | -3.87\% | 1.14\% | 3.61\% | 7.79\% | 3.42\% | 5.51\% | 7.22\% |
| GARCH (1,1)-T | -33.96\% | -24\% | -18.69\% | -422.84\% | -298.84\% | -232.75\% | -7.02\% | -4.96\% | -3.87\% | 0.19\% | 0.38\% | 0.38\% | 0.19\% | 0.38\% | 0.95\% |
| GARCH (1,1)- | -6.72\% | -6.17\% | -5.48\% | -79.11\% | $-72.62 \%$ | -64.55\% | -3.49\% | -3.20\% | -2.85\% | 5.51\% | 6.08\% | 7.98\% | 6.08\% | 7.22\% | 7.41\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| IGARCH (1,1)-N | -8.31\% | -5.88\% | -4.58\% | $-11.56 \%$ | -8.17\% | -6.37\% | -6.70\% | -4.74\% | -3.69\% | 1.14\% | 4.18\% | 6.84\% | 4.18\% | 6.84\% | 7.79\% |
| IGARCH (1,1)-T | -9.00\% | -6.36\% | -4.95\% | -36.09\% | -25.50\% | -19.86\% | -2.11\% | -1.49\% | -1.16\% | 1.52\% | 4.94\% | 7.60\% | 3.61\% | 5.89\% | 8.37\% |
| IGARCH (1,1)- | -5.93\% | -5.44\% | -4.84\% | -7.57\% | -6.94\% | -6.17\% | -5.15\% | -4.72\% | -4.19\% | 3.99\% | 5.32\% | 6.65\% | 6.84\% | 7.03\% | 7.41\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (GJR)TGARCH | -8.72\% | -6.17\% | -4.81\% | -42.59\% | -30.12\% | -23.47\% | -6.50\% | -4.60\% | -3.58\% | 1.52\% | 5.32\% | 8.37\% | 2.85\% | 5.13\% | 7.03\% |
| $(1,1)-\mathrm{N}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (GJR)TGARCH | - | - | - | -373.05\% | -263.65\% | - | $-14.74 \%$ | - | $-8.12 \%$ | 0.19\% | 0.38\% | 0.38\% | 0.19\% | 0.57\% | 1.14\% |
| (1,1)-T | 31.40\% | 22.19\% | 17.29\% |  |  | 205.35\% |  | 10.42\% |  |  |  |  |  |  |  |
| (GJR)TGARCH | -6.74\% | -6.19\% | -5.50\% | -71.55\% | -65.69\% | -58.39\% | -3.51\% | -3.23\% | -2.87\% | 5.70\% | 6.46\% | 8.17\% | 5.89\% | 6.84\% | 7.41\% |
| $(1,1)-\mathrm{GED}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| EGARCH (1,1)-N | -8.74\% | -6.18\% | -4.82\% | -77.38\% | -54.72\% | -42.65\% | -6.69\% | -4.73\% | -3.69\% | 1.52\% | 5.51\% | 8.56\% | 2.09\% | 5.32\% | 6.65\% |
| EGARCH (1,1)-T | - | - | - | - | - |  | -8.45\% | $-5.97 \%$ | $-4.65 \%$ | 0.38\% | 0.57\% | 2.09\% | 0.95\% | 1.71\% | 2.66\% |
|  | 20.85\% | 14.74\% | 11.48\% | 2144.37\% | 1515.51\% | 1180.37\% |  |  |  |  |  |  |  |  |  |
| EGARCH (1,1)- | -7.21\% | -6.62\% | -5.88\% | -432.87\% | -397.38\% | - | -3.50\% | -3.21\% | -2.86\% | 6.08\% | 7.22\% | 8.75\% | 5.70\% | 6.08\% | 7.22\% |
| GED |  |  |  |  |  | 353.23\% |  |  |  |  |  |  |  |  |  |
| APARCH (1,1)-N | -8.47\% | -5.99\% | -4.67\% | -18.35\% | -12.97\% | -10.11\% | $-2.50 \%$ | $-1.77 \%$ | $-1.38 \%$ | 2.28\% | 6.65\% | 9.70\% | 2.47\% | 5.51\% | 7.60\% |
| APARCH (1,1)-T | - | - | -8.03\% | -96.04\% | -67.88\% | -52.87\% | -5.04\% | -3.56\% | -2.77\% | 0.57\% | 1.33\% | 3.42\% | 1.14\% | 2.09\% | 3.42\% |
|  | 14.59\% | 10.31\% |  |  |  |  |  |  |  |  |  |  |  |  |  |
| APARCH (1,1)- | -5.96\% | -5.48\% | -4.87\% | -25.40\% | -23.32\% | -20.73\% | $-2.12 \%$ | -1.94\% | -1.73\% | 5.70\% | 7.22\% | 8.56\% | 5.89\% | 6.46\% | 7.22\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |


| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| TARCH (1,1)-X- | -8.73\% | -6.17\% | -4.81\% | -42.41\% | -29.99\% | -23.37\% | -6.55\% | -4.63\% | -3.61\% | 1.52\% | 5.32\% | 8.17\% | 2.85\% | 5.13\% | 7.22\% |
| N |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| TARCH (1,1)-X- | - | - | - | -246.18\% | -173.98\% | -135.51\% | -4.80\% | -3.39\% | $-2.64 \%$ | 0.19\% | 0.38\% | 0.76\% | 0.57\% | 1.33\% | 1.71\% |
| T | 21.70\% | 15.34\% | 11.94\% |  |  |  |  |  |  |  |  |  |  |  |  |
| TARCH (1,1)-X- | -6.67\% | -6.12\% | -5.44\% | -67.51\% | -61.98\% | -55.09\% | $-1.74 \%$ | -1.60\% | $-1.42 \%$ | 5.51\% | 6.27\% | 7.03\% | 6.08\% | 6.65\% | 7.41\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| RISK METRICS | - | - | -9.07\% | -211.23\% | -149.39\% | $-116.42 \%$ | -3.19\% | $-2.25 \%$ | -1.76\% | 0.95\% | 4.37\% | 6.46\% | $3.42 \%$ | 6.08\% | 7.41\% |
|  | 16.45\% | 11.63\% |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(100) Long | - | -5.59\% | -3.80\% | -275.11\% | -7.97\% | $-5.65 \%$ | $-5.33 \%$ | $-2.95 \%$ | $-2.11 \%$ | 1.52\% | 4.75\% | $11.03$ |  |  |  |
| position | 24.88\% |  |  |  |  |  |  |  |  |  |  | \% |  |  |  |
| HS(250) Long position | -8.81\% | $-5.04 \%$ | -3.33\% | $-12.70 \%$ | -6.70\% | -4.65\% | $-7.03 \%$ | -3.83\% | $-2.68 \%$ | 1.14\% | 5.32\% | $\begin{aligned} & 11.98 \\ & \% \end{aligned}$ |  |  |  |
| HS(FS) Long | -7.92\% | -4.35\% | $-2.99 \%$ | -8.39\% | -4.60\% | -3.12\% | $-7.32 \%$ | -4.20\% | $-2.92 \%$ | 1.71\% | 8.17\% | 13.69 |  |  |  |
| position |  |  |  |  |  |  |  |  |  |  |  | \% |  |  |  |
| HS(100) Short | 29.64\% | 7.44\% | 4.13\% | 9.54\% | 2.79\% | 1.52\% | 257.18 | 12.93\% | 7.37\% |  |  |  | 1.14\% | 4.56\% | 9.51\% |
| position |  |  |  |  |  |  | \% |  |  |  |  |  |  |  |  |
| HS(250) Short position | 14.11\% | 7.02\% | 3.32\% | 10.33\% | 4.26\% | 2.18\% | 15.75\% | 8.47\% | 4.68\% |  |  |  | 1.33\% | 5.51\% | 10.65\% |
| HS(FS) Short position | 11.22\% | 5.44\% | 3.33\% | 10.26\% | 5.37\% | 3.24\% | 12.31\% | 5.56\% | 3.43\% |  |  |  | 2.28\% | 7.03\% | 10.65\% |

Note: Table 2 represents out of sample observations. The number of observations is $526 . *$ denotes each confidence level at $1 \%, 5 \%$ or $10 \%$.

Table 3. Backtesting-TC2-Spot price returns-long positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1)-N | 0.101 | 2.351 | 3.052* |  | 0.135 | 4.177** |  | 2.486 | 7.229** | 8.003 | 7.838 | 7.764 |
| GARCH (1,1)-T | 5.234** | 39.457*** | 93.347*** |  |  |  |  |  |  | 101.585 | 56.868 | 38.078 |
| GARCH (1,1)-GED | $52.635 * * *$ | 1.220 | 2.532 | 0.288 | 0.626 | 0.744 | $52.923 * * *$ | 1.846 | 3.275 | 9.490 | 9.218 | 9.051 |
| IGARCH (1,1)-N | 0.101 | 0.782 | 6.473** |  | 3.356* | 6.858*** |  | 4.138 | 13.331 *** | 7.143 | 7.343 | 7.444 |
| $\operatorname{IGARCH}(1,1)-\mathrm{T}$ | 1.243 | 0.004 | 3.625* |  | 4.277** | 16.172*** |  | 4.281 | 19.798*** | 8.234 | 7.979 | 7.865 |
| IGARCH (1,1)-GED | 27.145*** | 0.113 | $7.331^{* * *}$ | 1.289 | 6.069** | 4.885** | $28.434^{* * *}$ | 6.182** | 12.216*** | 7.555 | 7.312 | 7.461 |
| (GJR) TGARCH (1,1)-N | 1.243 | 0.113 | 1.645 |  | 1.352 | 4.766** |  | 1.465 | $6.411^{* *}$ | 8.081 | 7.880 | 7.800 |
| (GJR)TGARCH $(1,1)-\mathrm{T}$ | 5.234** | 39.457*** | 93.347*** |  |  |  |  |  |  | 86.572 | 49.145 | 33.338 |
| (GJR)TGARCH (1,1)-GED | $56.178 * * *$ | 2.181 | 2.063 | 0.387 | 0.918 | 0.901 | $56.566^{* * *}$ | 3.099 | 2.964 | 9.554 | 9.282 | 9.105 |
| EGARCH (1,1)-N | 1.243 | 0.283 | 1.277 |  | 2.969* | 6.369** |  | 3.252 | 7.645** | 8.684 | 8.186 | 7.988 |
| EGARCH (1,1)-T | 2.672 | 34.644*** | $52.327 * * *$ |  |  |  |  |  |  | 511.207 | 260.309 | 161.20 |
| EGARCH (1,1)-GED | $63.476 * * *$ | 4.845** | 0.957 | 1.942 | 5.687** | 8.101*** | $65.418^{* * *}$ | 10.533*** | 9.058** | 29.399 | 26.135 | 22.456 |
| APARCH (1,1)-N | 6.402** | 2.757* | 0.055 |  | 7.496*** | 9.531*** |  | 10.253*** | 9.586*** | 7.561 | 7.594 | 7.620 |
| APARCH (1,1)-T | 1.161 | 20.805*** | 33.065*** |  |  |  |  |  |  | 13.912 | 11.302 | 9.976 |
| APARCH (1,1)-GED | 56.178*** | 4.845** | 1.277 | 0.387 | 1.782 | 4.289** | 56.566*** | 6.628** | 5.566* | 8.101 | 7.821 | 7.877 |
| TARCH (1,1)-X-N | 1.243 | 0.113 | 2.063 |  | 3.372* | 5.273** |  | 3.485 | 7.336** | 8.072 | 7.875 | 7.796 |
| TARCH (1,1)-X-T | 5.234** | 39.457*** | 81.415*** |  |  |  |  |  |  | 40.168 | 25.084 | 18.521 |
| TARCH (1,1)-X-GED | $52.635 * * *$ | 1.668 | 5.675** |  |  | 0.176 |  |  | 5.852* | 9.488 | 9.200 | 9.031 |
| RISK METRICS | 0.013 | 0.454 | 8.249*** |  | 2.942* | 5.410** |  | 3.396 | 13.659*** | 65.567 | 37.378 | 25.911 |
| HS(100) Long position | 1.243 | 0.069 | 0.598 | 8.418** | 4.784** | 14.129*** | 9.661*** | 4.853* | $14.728 * * *$ | 227.759 | 7.336 | 7.446 |
| HS(250) Long position | 0.101 | 0.113 | 2.163 | 3.808* | 13.145*** | 27.585*** | 3.908 | 13.258*** | 29.748*** | 7.134 | 7.302 | 7.410 |
| HS(FS) Long position | 2.215 | 9.445*** | 7.215*** | 2.215 | 13.256*** | 38.370*** | 4.430 | 22.701*** | 45.585*** | 7.147 | 7.353 | 7.462 |

Note: Table 3 represents out of sample observations. The number of observations is 526 . The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TC2 spot prices for long positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch. In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%$, $5 \%$ and $1 \%$. Critical values for Ch. In. are 9.21 , 5.99 and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.

Table 4. Backtesting-TC2-Spot price returns-short positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1)-N | 19.123*** | 0.283 | 4.936** |  | 2.969* | 5.687** |  | 3.252 | 10.623*** | 5.124 | 4.965 | 5.385 |
| GARCH (1,1)-T | 5.234** | $39.457 * * *$ | $76.301 * * *$ |  |  |  |  |  |  | 85.503 | 48.278 | 25.510 |
| GARCH (1,1)-GED | $63.476 * * *$ | 4.845** | 4.253** | 0.001 | 0.026 | 0.004 | 63.477*** | 4.871* | 4.257 | 6.355 | 4.788 | 5.028 |
| IGARCH (1,1)-N | 30.024*** | 3.394* | 3.052* | 1.056 | 20.735*** | 22.635*** | 31.080*** | 24.128*** | 25.687*** | 6.987 | 6.376 | 6.557 |
| IGARCH (1,1)-T | 21.689*** | 0.838 | 1.645 | 4.835** | 10.448*** | 22.763*** | 26.525*** | 11.287*** | 24.408*** | 6.615 | 6.104 | 6.282 |
| IGARCH (1,1)-GED | 78.855*** | 4.091** | 4.253** | 20.735*** | 23.717*** | 25.322*** | 99.590*** | 27.808*** | 29.575*** | 8.370 | 6.421 | 6.577 |
| (GJR)TGARCH (1,1)-N | $12.141^{* * *}$ | 0.019 | 5.675** |  | 0.267 | 3.933** |  | 0.286 | 9.608*** | 6.656 | 6.039 | 6.208 |
| (GJR)TGARCH (1,1)-T | 5.234** | $34.644^{* * *}$ | 71.592*** |  |  |  |  |  |  | 71.428 | 40.648 | 22.136 |
| (GJR)TGARCH (1,1)-GED | 59.793*** | 3.394* | 4.253** | 0.500 | 0.109 | 0.004 | 60.293*** | 3.503 | 4.257 | 6.775 | 5.189 | 5.372 |
| EGARCH (1,1)-N | 4.814** | 0.113 | 7.331 *** |  | 0.175 | 4.885** |  | 0.289 | 12.216*** | 6.958 | 6.118 | 6.219 |
| EGARCH (1,1)-T | 0.013 | 15.890*** | 43.203*** |  |  |  |  |  |  | 499.964 | 252.260 | 153.775 |
| EGARCH (1,1)-GED | $56.178 * * *$ | 1.220 | 4.936** | 0.909 | 0.561 | 0.590 | 57.087*** | 1.781 | 5.526* | 23.364 | 18.727 | 15.098 |
| APARCH (1,1)-N | 8.161*** | 0.283 | 3.625* |  | 2.969* | 6.982*** |  | 3.252 | 10.608*** | 7.020 | 6.318 | 6.464 |
| APARCH (1,1)-T | 0.101 | 11.887*** | 33.065*** |  |  |  |  |  |  | 7.161 | 6.906 | 6.591 |
| APARCH (1,1)-GED | 59.793*** | 2.181 | 4.936** | 0.017 | 1.394 | 1.782 | 59.810*** | 3.575 | 6.718** | 7.952 | 5.962 | 6.109 |
| TARCH ( 1,1 )-X-N | 12.141*** | 0.019 | 4.936** |  | 0.267 | 5.687** |  | 0.286 | 10.623*** | 6.683 | 6.062 | 6.222 |
| TARCH (1,1)-X-T | 1.161 | $20.805^{* * *}$ | 59.319*** |  |  |  |  |  |  | 23.246 | 14.920 | 10.887 |
| TARCH (1,1)-X-GED | 63.476*** | 2.757* | 4.253** | 0.626 | 0.057 | 0.004 | 64.102*** | 2.814 | 4.257 | 6.922 | 5.303 | 5.473 |
| RISK METRICS | 19.123*** | 1.220 | 4.253** | 5.419** | $13.180^{* * *}$ | 17.236*** | 24.542*** | 14.399*** | 21.489*** | 54.856 | 30.603 | 20.773 |
| HS(100) Short position | 0.101 | 0.218 | 0.145 | 3.808* | 8.806*** | 30.436*** | 3.908 | 9.024** | 30.581*** | 187.279 | 6.776 | 6.817 |
| HS(250) Short position | 0.527 | 0.283 | 0.240 |  | 16.275*** | 29.473*** |  | 16.558*** | 29.713*** | 6.172 | 6.470 | 6.635 |
| HS(FS) Short position | 6.402** | 4.091** | 0.240 | 1.229 | 23.717*** | 25.783*** | 7.631** | 27.808*** | 26.023*** | 6.138 | 6.461 | 6.657 |

Note: Table 4 represents out of sample observations. The number of observations is 526 . The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TC2 spot prices for short positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch. In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%, 5 \%$ and $1 \%$. Critical values for Ch. In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.
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Table 5. Value at Risk Statistics-TC2-One month front FFA price returns.

| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| GARCH (1,1)-N | -8.59\% | -6.07\% | -4.73\% | -10.79\% | -7.63\% | -5.94\% | $-7.42 \%$ | -5.25\% | -4.09\% | 2.47\% | 5.13\% | 8.94\% | 1.90\% | 4.75\% | 8.94\% |
| GARCH (1,1)-T | -9.10\% | -6.43\% | -5.01\% | -12.19\% | -8.62\% | -6.71\% | $-7.54 \%$ | -5.33\% | -4.15\% | 1.71\% | 4.37\% | 7.22\% | 1.52\% | 3.99\% | 7.22\% |
| GARCH (1,1)-GED | -6.07\% | -5.58\% | -4.96\% | -9.91\% | -9.10\% | -8.09\% | -4.96\% | -4.55\% | -4.05\% | 4.94\% | 6.46\% | 7.79\% | 5.13\% | 6.08\% | 7.98\% |
| IGARCH (1,1)-N | -8.72\% | -6.16\% | -4.80\% | -10.41\% | -7.36\% | -5.74\% | -6.70\% | -4.74\% | -3.69\% | 2.09\% | 5.51\% | 8.17\% | 1.90\% | 4.37\% | 8.37\% |
| IGARCH (1,1)-T | -8.83\% | -6.24\% | -4.86\% | -10.87\% | -7.68\% | -5.98\% | -6.63\% | -4.69\% | $-3.65 \%$ | 2.09\% | 5.32\% | 7.98\% | 1.90\% | 4.37\% | 7.79\% |
| IGARCH (1,1)- | -5.89\% | -5.40\% | -4.80\% | -6.56\% | -6.02\% | -5.35\% | -5.07\% | -4.65\% | -4.14\% | 5.70\% | 6.46\% | 8.94\% | 4.37\% | 5.51\% | 8.17\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \text { (GJR)TGARCH } \\ & (1,1)-\mathrm{N} \end{aligned}$ | -8.66\% | -6.13\% | -4.78\% | -10.15\% | -7.18\% | $-5.59 \%$ | $-7.63 \%$ | $-5.40 \%$ | -4.20\% | 2.09\% | 4.94\% | 8.56\% | 1.71\% | 4.18\% | 8.37\% |
| (GJR)TGARCH | -9.15\% | -6.47\% | -5.04\% | -22.74\% | - | $-12.52 \%$ | -7.93\% | -5.60\% | -4.36\% | 2.28\% | 4.94\% | 7.79\% | 1.71\% | 4.56\% | 7.98\% |
| $(1,1)-\mathrm{T}$ |  |  |  |  | 16.07\% |  |  |  |  |  |  |  |  |  |  |
| (GJR)TGARCH | -5.86\% | -5.37\% | -4.78\% | $-14.39 \%$ | - | $-11.74 \%$ | $-5.44 \%$ | -4.99\% | -4.44\% | 5.70\% | 6.84\% | 8.94\% | 5.32\% | 5.89\% | 8.75\% |
| $(1,1) \text {-GED }$ |  |  |  |  | $13.21 \%$ |  |  |  |  |  |  |  |  |  |  |
| EGARCH (1,1)-N | -8.96\% | -6.33\% | -4.94\% | -10.37\% | -7.33\% | $-5.71 \%$ | $-7.31 \%$ | -5.17\% | -4.03\% | 1.90\% | 4.56\% | 7.41\% | 1.71\% | 4.18\% | 7.98\% |
| EGARCH (1,1)-T | -9.46\% | -6.69\% | -5.21\% | -12.31\% | -8.70\% | -6.78\% | $-7.44 \%$ | -5.26\% | -4.10\% | 1.33\% | 4.18\% | 7.03\% | 1.14\% | 3.99\% | 6.65\% |
| EGARCH (1,1)- | -6.43\% | -5.91\% | -5.25\% | -8.75\% | -8.03\% | -7.14\% | -4.94\% | -4.53\% | -4.03\% | 4.75\% | 5.51\% | 6.84\% | 3.99\% | 5.13\% | 6.65\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| APARCH (1,1)-N | -8.97\% | -6.34\% | -4.94\% | -10.41\% | $-7.36 \%$ | -5.74\% | $-7.31 \%$ | -5.17\% | -4.03\% | 1.90\% | 4.56\% | 7.41\% | 1.71\% | 4.18\% | 7.98\% |
| APARCH (1,1)-T | -9.62\% | -6.80\% | -5.30\% | -12.52\% | -8.85\% | -6.89\% | $-7.37 \%$ | -5.21\% | -4.05\% | 1.52\% | 4.37\% | 6.84\% | 1.14\% | 3.80\% | 6.65\% |
| APARCH (1,1)- | -6.54\% | -6.00\% | -5.34\% | -8.62\% | -7.91\% | -7.04\% | -5.35\% | -4.91\% | -4.36\% | 4.37\% | 5.13\% | 6.84\% | 3.80\% | 4.75\% | 6.65\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| TARCH (1,1)-X-N | -8.61\% | -6.09\% | -4.74\% | $-10.69 \%$ | -7.56\% | -5.89\% | $-7.42 \%$ | $-5.25 \%$ | -4.09\% | 2.28\% | 5.13\% | 8.37\% | 1.90\% | 4.75\% | 8.56\% |
| TARCH (1,1)-X-T | -9.15\% | -6.46\% | -5.03\% | -22.90\% | - | $-12.61 \%$ | -7.91\% | $-5.59 \%$ | -4.36\% | 2.09\% | 4.94\% | 7.79\% | 1.71\% | 4.75\% | 7.98\% |
|  |  |  |  |  | $16.19 \%$ |  |  |  |  |  |  |  |  |  |  |
| TARCH (1,1)-X- | $-5.97 \%$ | -5.48\% | -4.87\% | $-15.09 \%$ | - | $-12.31 \%$ | $-5.44 \%$ | $-5.00 \%$ | -4.44\% | 5.70\% | 6.84\% | 8.37\% | 5.32\% | 5.70\% | 8.37\% |
| GED |  |  |  |  | 13.85\% |  |  |  |  |  |  |  |  |  |  |


| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| RISK METRICS | -8.98\% | -6.35\% | -4.95\% | -16.18\% | $-11.44 \%$ | -8.92\% | -5.42\% | -3.83\% | -2.99\% | 2.28\% | 5.32\% | 8.37\% | 1.90\% | 4.56\% | 8.75\% |
| HS(100) Long | - | -6.33\% | -4.28\% | -21.65\% | -9.02\% | $-5.56 \%$ | -8.09\% | $-4.21 \%$ | -2.96\% | 0.76\% | 5.70\% | 11.41\% |  |  |  |
| position | 12.90\% |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(250) Long | - | -6.08\% | -3.98\% | -16.45\% | -9.28\% | -4.92\% | - | $-5.31 \%$ | $-2.84 \%$ | 0.38\% | 5.51\% | 12.55\% |  |  |  |
| position | 13.76\% |  |  |  |  |  | 11.87\% |  |  |  |  |  |  |  |  |
| HS(FS) Long | - | -5.06\% | -3.58\% | -11.12\% | $-5.25 \%$ | -3.69\% | - | $-4.92 \%$ | $-3.42 \%$ | 1.14\% | 7.60\% | 14.26\% |  |  |  |
| position | 11.09\% |  |  |  |  |  | 11.01\% |  |  |  |  |  |  |  |  |
| HS(100) Short position | 12.47\% | 6.14\% | 4.38\% | 5.44\% | 3.36\% | 2.96\% | 20.91\% | 8.80\% | 5.58\% |  |  |  | 1.90\% | 5.70\% | 10.27\% |
| HS(250) Short position | 10.09\% | 5.17\% | 4.09\% | 6.54\% | 3.92\% | 3.25\% | 12.85\% | 6.41\% | 5.02\% |  |  |  | 1.71\% | 7.03\% | 12.55\% |
| HS(FS) Short position | 9.36\% | 4.98\% | 3.65\% | 9.21\% | 4.83\% | 3.47\% | 9.48\% | 5.10\% | 3.84\% |  |  |  | 1.33\% | 7.79\% | 14.64\% |

Note: Table 5 represents out of sample observations. The number of observations is 526 . denotes each confidence level at $1 \%, 5 \%$ or $10 \%$.

Table 6. Backtesting-TC2-One month front FFA price returns-Long positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1)-N | 8.161*** | 0.019 | 0.685 |  | 1.612 | 0.930 |  | 1.631 | 1.615 | 0.390 | 0.107 | 0.145 |
| GARCH (1,1)-T | 2.215 | 0.454 | 4.936** |  |  | 1.928 |  |  | 6.864** | 0.293 | 0.153 | 0.178 |
| GARCH (1,1)-GED | 42.451*** | 2.181 | 3.052* | 0.379 | 1.394 | 1.151 | $42.831^{* * *}$ | 3.575 | 4.203 | 1.359 | 0.101 | 0.181 |
| IGARCH (1,1)-N | 4.814** | 0.283 | 2.063 |  | 0.244 | 1.913 |  | 0.527 | 3.976 | 0.378 | 0.124 | 0.157 |
| IGARCH (1,1)-T | 4.814** | 0.113 | 2.532 |  | 0.166 | 2.220 |  | 0.279 | 4.752* | 0.363 | 0.137 | 0.166 |
| $\text { IGARCH }(1,1) \text {-GED }$ | 56.178*** | 2.181 | $0.685$ | 0.909 | 3.331* | 2.084 | $57.087 * * *$ | 5.512* | 2.768 | 1.427 | 0.077 | 0.148 |
| (GJR)TGARCH (1,1)-N | 4.814** | 0.004 | 1.277 |  | $0.379$ | 1.374 |  | 0.383 | $2.651$ | $0.362$ | $0.109$ | $0.148$ |
| (GJR)TGARCH (1,1)-T | 6.402** | 0.004 | 3.052* |  | 1.899 | 2.553 |  | 1.903 | 5.605* | 0.348 | 0.191 | 0.204 |
| (GJR)TGARCH (1,1)-GED | $56.178 * * *$ | 3.394* | 0.685 | 0.909 | 4.393** | 2.084 | $57.087 * * *$ | 7.787** | 2.768 | 1.465 | 0.099 | 0.164 |
| EGARCH (1,1)-N | 3.412* | 0.218 | 4.253** |  | 0.010 | 3.300* |  | 0.228 | 7.553** | 0.296 | 0.128 | 0.164 |
| EGARCH (1,1)-T | 0.527 | 0.782 | 5.675** |  |  | 2.238 |  |  | 7.913** | 0.226 | $0.186$ | $0.204$ |
| $\text { EGARCH }(1,1) \text {-GED }$ | 39.215*** | 0.283 | 6.473** | 0.035 | 1.233 | 2.574 | $39.251^{* * *}$ | 1.515 | 9.047** | 1.178 | 0.109 | 0.212 |
| APARCH (1,1)-N | 3.412* | 0.218 | 4.253** |  | 0.010 | 3.300* |  | 0.228 | 7.553** | 0.294 | 0.129 | 0.164 |
| APARCH (1,1)-T | 1.243 | 0.454 | 6.473** |  | 0.000 | 2.574 |  | 0.454 | 9.047** | 0.202 | 0.202 | 0.216 |
| APARCH (1,1)-GED | 32.998*** | 0.019 | 6.473** | 0.000 | 1.612 | 2.574 | $32.998 * * *$ | 1.631 | 9.047** | 1.123 | 0.106 | 0.217 |
| TARCH (1,1)-X-N | 6.402** | 0.019 | 1.645 |  | 3.807* | 1.632 |  | 3.827 | 3.277 | 0.392 | 0.115 | 0.151 |
| TARCH (1,1)-X-T | 4.814** | 0.004 | 3.052* |  | 1.899 | 2.553 |  | 1.903 | 5.605* | 0.352 | 0.193 | 0.205 |
| TARCH (1,1)-X-GED | $56.178 * * *$ | 3.394* | 1.645 | 0.909 | 4.393** | 3.124* | $57.087 * * *$ | 7.787** | 4.769* | 1.409 | 0.104 | 0.177 |
| RISK METRICS | 6.402** | 0.113 | 1.645 |  | 0.166 | 0.050 |  | 0.279 | 1.695 | 0.518 | 0.247 | 0.237 |
| HS(100) Long position | 0.332 | 0.525 | 1.112 |  | 0.909 | 1.804 |  | 1.434 | 2.916 | 1.299 | 0.206 | 0.140 |
| HS(250) Long position | 2.672 | 0.283 | 3.539* |  | 2.969* | 0.508 |  | 3.252 | 4.047 | 0.583 | 0.109 | 0.120 |
| HS(FS) Long position | 0.101 | 6.524** | 9.493*** |  | 4.898** | 0.255 |  | 11.422*** | 9.747*** | 0.015 | 0.078 | 0.122 |

Note: Table 6 represents out of sample observations. The number of observations is 526. The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TC2 One month front Forward Freight Agreements prices for long positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch. In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ${ }^{* *}$ and ${ }^{* * *}$ denote significance level at $10 \%, 5 \%$ and $1 \%$. Critical values for Ch . In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.
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Table 7. Backtesting-TC2-One month front FFA price returns-Short positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1)-N | 3.412* | 0.069 | 0.685 |  | 2.216 | 0.930 |  | 2.284 | 1.615 | 0.100 | 0.119 | 0.130 |
| GARCH (1,1)-T | 1.243 | 1.204 | 4.936** |  | 1.289 | 0.671 |  | 2.493 | 5.607* | 0.091 | 0.168 | 0.159 |
| GARCH (1,1)-GED | 45.769*** | 1.220 | 2.532 | 0.267 | 0.561 | 0.176 | 46.035*** | 1.781 | 2.708 | 0.659 | 0.103 | 0.159 |
| $\operatorname{IGARCH}(1,1)-\mathrm{N}$ | 3.412* | 0.454 | 1.645 |  | 2.942* | 1.632 |  | 3.396 | 3.277 | 0.110 | 0.142 | 0.146 |
| IGARCH (1,1)-T | 3.412* | 0.454 | 3.052* |  | 2.942* | 1.151 |  | 3.396 | 4.203 | 0.115 | 0.155 | 0.153 |
| IGARCH (1,1)-GED | 32.998*** | 0.283 | 2.063 | 2.942* | 1.118 | 0.751 | 35.940 *** | 1.400 | 2.814 | 0.709 | 0.083 | 0.135 |
| (GJR) TGARCH (1,1)-N | 2.215 | 0.782 | 1.645 |  | 3.356* | 1.632 |  | 4.138 | 3.277 | 0.080 | 0.120 | 0.132 |
| (GJR) TGARCH (1,1)-T | 2.215 | 0.218 | 2.532 |  | 0.670 | 0.029 |  | 0.888 | 2.561 | 0.159 | 0.209 | 0.186 |
| (GJR) TGARCH (1,1)-GED | 49.164*** | 0.838 | 0.957 | 0.175 | 0.017 | 1.141 | 49.339*** | 0.856 | 2.097 | 0.734 | 0.098 | 0.144 |
| EGARCH (1,1)-N | 2.215 | 0.782 | 2.532 |  | 3.356* | 0.176 |  | 4.138 | 2.708 | 0.068 | 0.145 | 0.146 |
| $\text { EGARCH }(1,1)-\mathrm{T}$ | 0.101 | 1.204 | 7.331 *** |  | 1.289 | 1.158 |  | 2.493 | 8.488** | 0.085 | 0.203 | 0.181 |
| EGARCH (1,1)-GED | 27.145*** | 0.019 | 7.331*** | 1.289 | 1.612 | 1.158 | 28.434*** | 1.631 | 8.488** | 0.543 | 0.117 | 0.189 |
| APARCH (1,1)-N | 2.215 | 0.782 | 2.532 |  | 3.356* | 0.176 |  | 4.138 | 2.708 | 0.069 | 0.146 | 0.147 |
| APARCH (1,1)-T | 0.101 | 1.726 | 7.331*** |  | 1.550 | 1.158 |  | 3.276 | 8.488** | 0.088 | 0.222 | 0.192 |
| APARCH (1,1)-GED | $24.365 * * *$ | 0.069 | 7.331 *** | 1.550 | 2.216 | 1.158 | $25.915^{* * *}$ | 2.284 | 8.488** | 0.500 | 0.114 | 0.191 |
| TARCH (1,1)-X-N | 3.412* | 0.069 | 1.277 |  | 2.216 | 0.441 |  | 2.284 | 1.718 | 0.101 | 0.120 | 0.130 |
| TARCH (1,1)-X-T | 2.215 | 0.069 | 2.532 |  | 0.513 | 0.029 |  | 0.582 | 2.561 | 0.160 | 0.209 | 0.186 |
| TARCH (1,1)-X-GED | 49.164*** | 0.525 | 1.645 | 0.175 | 0.051 | 0.050 | $49.339^{* * *}$ | 0.576 | 1.695 | 0.697 | 0.104 | 0.156 |
| RISK METRICS | 3.412* | 0.218 | 0.957 |  | 0.010 | 1.141 |  | 0.228 | 2.097 | 0.303 | 0.261 | 0.213 |
| HS(100) Short position | 3.412* | 0.525 | 0.041 |  | 2.598 | 1.330 |  | 3.123 | 1.372 | 26.432 | 6.530 | 3.330 |
| HS(250) Short position | 2.215 | 4.091** | 3.539* | 2.215 | 0.757 | 3.310* | 4.430 | 4.847* | 6.849** | 19.917 | 5.275 | 3.023 |
| HS(FS) Short position | $0.527$ | 7.445*** | 11.168*** |  | 0.006 | 3.814* |  | 7.451** | 14.982*** | 18.402 | 5.010 | 2.634 |

Note: Table 7 represents out of sample observations. The number of observations is 526. The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TC2 One month front Forward Freight Agreements prices for short positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%$, $5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%$, $10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.

Table 8. Value at Risk Statistics-TC2-three months front FFA price returns.


| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| APARCH (1,1)-T | -7.68\% | -5.43\% | -4.23\% | $-14.23 \%$ | -10.06\% | -7.83\% | -4.96\% | -3.51\% |  | 0.95\% | 1.90\% | 3.23\% | 0.95\% | 1.90\% | 2.85\% |
|  |  |  |  |  |  |  |  |  | 2.73\% |  |  |  |  |  |  |
| APARCH (1,1)-GED | -3.12\% | $-2.87 \%$ | $-2.55 \%$ | -7.15\% | -6.56\% | -5.83\% | $-2.49 \%$ | $-2.29 \%$ | - | 5.32\% | 6.46\% | 7.98\% | 5.51\% | 6.84\% | 7.60\% |
|  |  |  |  |  |  |  |  |  | 2.03\% |  |  |  |  |  |  |
| TARCH (1,1)-X-N | $-5.45 \%$ | -3.86\% | $-3.01 \%$ | $-27.23 \%$ | -19.26\% | -15.01\% | $-4.14 \%$ | $-2.93 \%$ |  | 2.28\% | 3.99\% | 6.46\% | 2.28\% | 4.37\% | 7.03\% |
|  |  |  |  |  |  |  |  |  | 2.28\% |  |  |  |  |  |  |
| TARCH (1,1)-X-T | $-7.03 \%$ | $-4.97 \%$ | -3.87\% | $-10.44 \%$ | -7.38\% | -5.75\% | -5.91\% | -4.17\% |  | 1.52\% | 1.90\% | 3.80\% | 1.14\% | 2.09\% | 3.23\% |
|  |  |  |  |  |  |  |  |  | 3.25\% |  |  |  |  |  |  |
| TARCH (1,1)-X- | $-3.00 \%$ | $-2.75 \%$ | $-2.44 \%$ | -6.76\% | -6.21\% | -5.52\% | $-2.45 \%$ | $-2.25 \%$ | - | 6.27\% | 7.03\% | 7.98\% | 6.08\% | 7.03\% | 8.17\% |
| GED |  |  |  |  |  |  |  |  | 2.00\% |  |  |  |  |  |  |
| RISK METRICS | -5.19\% | $-3.67 \%$ | -2.86\% | -13.39\% | -9.47\% | -7.38\% | $-2.39 \%$ | $-1.69 \%$ | - | 2.85\% | 5.32\% | 7.03\% | 2.47\% | 4.56\% | 7.22\% |
|  |  |  |  |  |  |  |  |  | $1.32 \%$ |  |  |  |  |  |  |
| HS(100) Long position | -9.32\% | -3.49\% | $-2.15 \%$ | $-14.81 \%$ | -6.80\% | -4.07\% | -3.11\% | $-1.53 \%$ | $-$ | 1.52\% | 5.13\% | 10.46\% |  |  |  |
|  |  |  |  |  |  |  |  |  | 1.35\% |  |  |  |  |  |  |
| HS(250) Long position | $-8.44 \%$ | -3.18\% | $-1.84 \%$ | -12.38\% | $-4.24 \%$ | $-2.59 \%$ | $-4.84 \%$ | -1.93\% |  | 1.33\% | 5.70\% | 11.41\% |  |  |  |
|  |  |  |  |  |  |  |  |  | 1.51\% |  |  |  |  |  |  |
| HS(FS) Long position | $-5.87 \%$ | -2.74\% | $-1.86 \%$ | -6.13\% | $-2.79 \%$ | $-1.89 \%$ | -5.72\% | -2.68\% |  | 1.71\% | 6.27\% | 10.84\% |  |  |  |
|  |  |  |  |  |  |  |  |  | 1.83\% |  |  |  |  |  |  |
| HS(100) Short position | 9.52\% | 3.37\% | 2.25\% | 2.59\% | 1.96\% | 1.49\% | 16.11\% | 5.32\% | 3.64\% |  |  |  | 1.33\% | 4.75\% | 9.70\% |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(250) Short position | 6.36\% | 2.94\% | 1.91\% | 3.14\% | 2.45\% | 1.47\% | 8.94\% | 4.41\% | 2.69\% |  |  |  | 2.09\% | 6.84\% | 11.22\% |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(FS) Short position | 5.05\% | 2.80\% | 1.94\% | 4.88\% | 2.71\% | 1.92\% | 5.32\% | 2.87\% | 1.98\% |  |  |  | 2.09\% | 6.65\% | 11.60\% |

Note: Table 8 represents out of sample observations. The number of observations is $526 . *$ denotes each confidence level at $1 \%, 5 \%$ or $10 \%$.

Table 9. Backtesting-TC2-three months front FFA price returns-Long positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1)-N | 0.527 | 1.726 | 10.277*** |  |  | 0.001 |  |  | 10.278*** | 0.191 | 0.162 | 0.143 |
| GARCH (1,1)-T | 0.527 | 13.786*** | 28.716*** |  | 1.836 | 0.074 |  | 15.622*** | 28.789*** | 0.128 | 0.327 | 0.268 |
| GARCH (1,1)-GED | 82.853*** | 8.419*** | 1.645 | 2.238 | 2.220 | 1.632 | 85.091 *** | 10.639*** | 3.277 | 0.614 | 0.074 | 0.081 |
| $\operatorname{IGARCH}(1,1)-\mathrm{N}$ | 6.402** | 0.218 | 8.249*** | 1.229 | 0.758 | 1.522 | 7.631** | 0.976 | 9.772*** | 0.161 | 0.115 | 0.116 |
| $\operatorname{IGARCH}(1,1)-\mathrm{T}$ | 6.402** | 0.218 | 8.249*** | 1.229 | 0.758 | 1.522 | 7.631** | 0.976 | 9.772*** | 0.161 | 0.119 | 0.119 |
| $\text { IGARCH }(1,1)-G E D$ | 52.635*** | 0.525 | 3.625* | 0.104 | 0.051 | 1.265 | $52.738 * * *$ | 0.576 | 4.890* | 0.518 | 0.052 | 0.075 |
| (GJR)TGARCH (1,1)-N | 6.402** | 1.204 | 8.249*** |  |  | 0.918 |  |  | 9.167** | 0.379 | 0.266 | 0.214 |
| (GJR)TGARCH (1,1)-T | 0.527 | 13.786*** | 28.716*** |  | 1.836 | 0.074 |  | 15.622*** | 28.789*** | 0.105 | 0.299 | 0.250 |
| (GJR)TGARCH (1,1)-GED | 39.215*** | 0.019 | 10.277*** | 0.513 | 1.612 | 4.209** | 39.728*** | 1.631 | 14.486*** | 0.397 | 0.122 | 0.159 |
| EGARCH (1,1)-N | 3.412* | 0.782 | 4.936** |  | 0.007 | 1.928 |  | 0.789 | 6.864** | 0.170 | 0.136 | 0.131 |
| EGARCH (1,1)-T | 1.243 | 11.887*** | $21.230^{* * *}$ |  | 1.510 | 0.670 |  | 13.397*** | 21.900 *** | 0.128 | 0.292 | 0.242 |
| EGARCH (1,1)-GED | 82.853*** | 6.524** | 0.459 | 0.757 | 1.265 | 3.223* | 83.610*** | 7.788** | 3.683 | 0.610 | 0.064 | 0.072 |
| APARCH (1,1)-N | $12.141^{* * *}$ | 0.454 | 4.253** | 0.598 | 0.000 | 1.644 | 12.739*** | 0.454 | 5.897* | 0.178 | 0.117 | 0.117 |
| APARCH (1,1)-T | 0.013 | 13.786*** | 35.409*** |  | 1.836 | 0.320 |  | 15.622*** | 35.729*** | 0.270 | 0.450 | 0.350 |
| APARCH (1,1)-GED | 49.164*** | 2.181 | 2.532 | 0.175 | 3.130* | 2.220 | 49.339*** | 5.311* | 4.752* | 0.511 | 0.062 | 0.086 |
| TARCH (1,1)-X-N | 6.402** | 1.204 | 8.249*** |  |  | 0.918 |  |  | 9.167** | 0.362 | 0.258 | 0.210 |
| TARCH (1,1)-X-T | 1.243 | 13.786*** | 28.716*** |  | 1.836 | 0.074 |  | 15.622*** | 28.789*** | 0.105 | 0.297 | 0.248 |
| TARCH (1,1)-X-GED | 67.226*** | 4.091** | 2.532 | 1.655 | 2.079 | 2.220 | 68.881*** | 6.169** | 4.752* | 0.544 | 0.062 | 0.080 |
| RISK METRICS | $12.141^{* * *}$ | 0.113 | 5.675** | 0.598 | 6.375** | 4.161** | 12.739*** | 6.489** | 9.836*** | 0.268 | 0.177 | 0.154 |
| HS(100) Long position | 1.243 | 0.019 | 0.120 |  | 4.040** | 3.549* |  | 4.060 | 3.669 | 1.271 | 0.168 | 0.092 |
| HS(250) Long position | 0.527 | 0.525 | 1.112 |  | 0.909 | 8.164*** |  | 1.434 | 9.276*** | 0.634 | 0.074 | 0.079 |
| HS(FS) Long position | 2.215 | 1.668 | 0.399 | 2.215 | 0.420 | 6.009** | 4.430 | 2.089 | 6.408** | 0.024 | 0.053 | 0.071 |

Note: Table 9 represents out of sample observations. The number of observations is 526. The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TC2 Three months front Forward Freight Agreements prices for long positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%$, $5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.

Table 10. Backtesting-TC2-three months front FFA price returns-Short positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1) - N | 3.412* | 1.204 | 11.390*** |  |  | 0.500 |  |  | 11.890*** | 0.167 | 0.158 | 0.143 |
| $\operatorname{GARCH}(1,1)-\mathrm{T}$ | 0.013 | 11.887*** | 40.470*** |  |  |  |  |  |  | 0.260 | 0.312 | 0.254 |
| GARCH (1,1) - GED | 82.853*** | 4.845** | 0.120 | 0.176 | 0.259 | 0.012 | 83.030*** | 5.105* | 0.132 | 0.383 | 0.078 | 0.079 |
| IGARCH (1,1) - N | 6.402** | 1.726 | 8.249*** |  |  | 0.022 |  |  | 8.271** | 0.115 | 0.112 | 0.110 |
| IGARCH (1,1)- T | 8.161*** | 1.726 | 10.277*** |  |  | 0.626 |  |  | 10.903*** | 0.119 | 0.116 | 0.112 |
| $\operatorname{IGARCH}(1,1)-\mathrm{GED}$ | 52.635*** | 1.668 | 1.645 | 0.104 | 0.420 | 0.510 | 52.738*** | 2.089 | 2.155 | 0.303 | 0.051 | 0.068 |
| (GJR)TGARCH $(1,1)-\mathrm{N}$ | 10.077*** | 0.454 | 5.675** |  | 0.000 | 0.176 |  | 0.454 | 5.852* | 0.348 | 0.249 | 0.198 |
| (GJR)TGARCH ( 1,1 ) - T | 0.101 | 13.786*** | 37.875*** |  |  |  |  |  |  | 0.219 | 0.282 | 0.233 |
| (GJR)TGARCH (1,1) - GED | 42.451*** | 0.004 | $12.571^{* * *}$ |  |  |  |  |  |  | 0.242 | 0.125 | 0.156 |
| EGARCH (1,1) - N | 3.412* | 0.004 | 4.253** |  | 0.076 | 0.446 |  | 0.080 | 4.699* | 0.127 | 0.123 | 0.118 |
| EGARCH (1,1) - T | 0.527 | 10.173*** | 28.716*** |  |  |  |  |  |  | 0.233 | 0.278 | 0.229 |
| EGARCH (1,1) - GED | 67.226*** | $8.419^{* * *}$ | 0.145 | 0.003 | 0.047 | 0.156 | 67.229*** | 8.466** | 0.301 | 0.380 | 0.067 | 0.070 |
| APARCH (1,1) - N | 3.412* | 0.019 | 1.645 |  | 0.267 | 0.031 |  | 0.286 | 1.676 | 0.121 | 0.107 | 0.106 |
| APARCH (1,1) - T | 0.013 | 13.786*** | 40.470*** |  |  |  |  |  |  | 0.444 | 0.435 | 0.334 |
| APARCH (1,1) - GED | 52.635*** | 3.394* | 3.625* | 0.288 | 0.109 | 0.001 | 52.923*** | 3.503 | 3.626 | 0.301 | 0.064 | 0.081 |
| TARCH (1,1) - X - N | 6.402** | 0.454 | 5.675** |  | 0.000 | 0.066 |  | 0.454 | 5.741* | 0.328 | 0.237 | 0.191 |
| TARCH (1,1) - X - T | 0.101 | 11.887*** | 35.409*** |  |  |  |  |  |  | 0.219 | 0.281 | 0.232 |
| TARCH $(1,1)-\mathrm{X}$ - GED | 63.476*** | 4.091** | 2.063 | 0.001 | 0.176 | 0.096 | $63.477 * * *$ | 4.267 | 2.159 | 0.327 | 0.065 | 0.077 |
| RISK METRICS | 8.161*** | 0.218 | 4.936** |  |  | 0.259 |  |  | 5.195* | 0.234 | 0.175 | 0.149 |
| HS(100) Short position | 0.527 | 0.069 | 0.055 |  |  | 0.257 |  |  | 0.312 | 2.009 | 0.106 | 0.081 |
| HS(250) Short position | 4.814** | 3.394* | 0.836 |  | 0.125 | 0.342 |  | 3.518 | 1.178 | 0.219 | 0.071 | 0.076 |
| HS(FS) Short position | 4.814** | 2.757* | 1.425 |  | 1.158 | 0.001 |  | 3.915 | 1.427 | 0.030 | 0.051 | 0.068 |

Note: Table 10 represents out of sample observations. The number of observations is 526 . The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TC2 Three months front Forward Freight Agreements prices for short positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%$, $5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.
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Table 11. Value at Risk Statistics-TD3-Spot price returns.

| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| GARCH (1,1) - N | -8.96\% | -6.34\% | -4.94\% | -41.18\% | -29.12\% | -22.70\% | -4.88\% | -3.45\% | $-2.69 \%$ | 1.14\% | 3.80\% | 6.27\% | 1.33\% | 4.37\% | 7.03\% |
| $\operatorname{GARCH}(1,1)-\mathrm{T}$ | - | - | - | - | - | - | - | - | - | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% |
|  | 338.98\% | 239.57\% | 186.59\% | 2535.35\% | 1791.84\% | 1395.59\% | 131.88\% | 93.21\% | 72.59\% |  |  |  |  |  |  |
| GARCH (1,1) - | -6.90\% | -6.30\% | -5.60\% | -45.09\% | -41.21\% | -36.63\% | -2.87\% | $-2.62 \%$ | $-2.33 \%$ | 3.42\% | 3.99\% | 5.89\% | 3.61\% | 3.99\% | 5.51\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| IGARCH (1,1) - N | -8.02\% | -5.67\% | -4.42\% | -15.53\% | -10.98\% | -8.56\% | -3.72\% | $-2.63 \%$ | $-2.05 \%$ | 2.09\% | 3.99\% | 6.84\% | 2.66\% | 5.89\% | 8.75\% |
| IGARCH (1,1) - T | -7.60\% | -5.37\% | -4.18\% | -22.54\% | $-15.93 \%$ | -12.41\% | -2.08\% | -1.47\% | -1.14\% | 2.28\% | 5.32\% | 7.41\% | 3.42\% | 7.41\% | 10.27\% |
| IGARCH (1,1) - | -5.67\% | -5.18\% | -4.61\% | -14.93\% | -13.62\% | -12.10\% | -1.95\% | -1.78\% | $-1.58 \%$ | 4.18\% | 5.13\% | 6.27\% | 6.08\% | 7.79\% | 9.70\% |
| GED |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (GJR)TGARCH | -8.99\% | -6.36\% | -4.95\% | -42.44\% | -30.02\% | -23.39\% | -4.86\% | -3.43\% | $-2.68 \%$ | 1.14\% | 4.18\% | 6.46\% | 1.33\% | 4.18\% | 7.03\% |
| $(1,1)-\mathrm{N}$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| (GJR)TGARCH | - | - | - | - | - | - | - | - | - | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% |
| (1,1) - T | 324.49\% | 229.33\% | 178.62\% | 2376.37\% | 1679.48\% | 1308.07\% | 126.09\% | 89.11\% | 69.41\% |  |  |  |  |  |  |
| (GJR)TGARCH | -6.88\% | -6.29\% | -5.59\% | -44.25\% | -40.44\% | -35.95\% | -2.88\% | $-2.63 \%$ | $-2.34 \%$ | 3.42\% | 3.99\% | 5.70\% | 3.61\% | 4.18\% | 5.70\% |
| $(1,1)-\text { GED }$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| EGARCH (1,1) - N | -8.93\% | -6.31\% | -4.92\% | -59.01\% | -41.73\% | -32.52\% | -4.04\% | -2.86\% | $-2.23 \%$ | 0.95\% | 3.99\% | 6.27\% | 1.90\% | 3.99\% | 6.84\% |
| EGARCH (1,1)- T | -21.57\% | $-15.24 \%$ | -11.87\% | -332.53\% | -235.01\% | -183.04\% | -8.61\% | - | - | 0.00\% | 0.00\% | 0.19\% | 0.19\% | 0.57\% | 0.95\% |
|  |  |  |  |  |  |  |  | $6.08 \%$ | 4.74\% |  |  |  |  |  |  |
| EGARCH (1,1) - | -6.46\% | -5.90\% | $-5.24 \%$ | -76.98\% | -70.36\% | -62.54\% | $-2.72 \%$ | -2.47\% | - | 3.61\% | 4.37\% | 6.08\% | 3.99\% | 5.32\% | 6.08\% |
| GED |  |  |  |  |  |  |  |  | 2.20\% |  |  |  |  |  |  |
| APARCH (1,1) - N | -8.95\% | $-6.33 \%$ | -4.93\% | -37.13\% | -26.26\% | -20.46\% | -4.51\% | -3.19\% | - | 0.76\% | 3.80\% | 6.27\% | 1.52\% | 3.99\% | 7.41\% |
|  |  |  |  |  |  |  |  |  | 2.49\% |  |  |  |  |  |  |
| APARCH (1,1)-T | - | - | -26.90\% | -264.53\% | -186.95\% | -145.61\% | $-14.77 \%$ | - | - | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% |
|  | 48.87\% | 34.54\% |  |  |  |  |  | 10.44\% | 8.13\% |  |  |  |  |  |  |
| APARCH (1,1) - | $-6.69 \%$ | -6.11\% | $-5.43 \%$ | -32.82\% | -29.97\% | -26.64\% | $-2.28 \%$ | -2.09\% | - | 3.23\% | 3.80\% | 5.51\% | 4.37\% | 4.94\% | 5.13\% |
| GED |  |  |  |  |  |  |  |  | 1.85\% |  |  |  |  |  |  |


| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| TARCH (1,1) - X - | -9.21\% | -6.52\% | -5.08\% | -47.23\% | -33.40\% | -26.03\% | -4.15\% | -2.93\% | - | 0.95\% | 3.99\% | 6.46\% | 1.33\% | 3.80\% | 6.84\% |
| N |  |  |  |  |  |  |  |  | 2.29\% |  |  |  |  |  |  |
| $\text { TARCH }(1,1)-\mathrm{X}-\mathrm{T}$ | - | - | - | - | - | - | - | - | - | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% | 0.00\% |
|  | 301.49\% | 213.08\% | 165.96\% | 2210.88\% | 1562.52\% | 1216.98\% | 103.54\% | 73.18\% | 56.99\% |  |  |  |  |  |  |
| TARCH (1,1) - X - | -6.90\% | -6.30\% | -5.60\% | -44.59\% | -40.75\% | -36.22\% | $-2.58 \%$ | $-2.35 \%$ | - | 3.42\% | 4.56\% | 5.32\% | 3.23\% | 4.18\% | 5.89\% |
| GED |  |  |  |  |  |  |  |  | 2.09\% |  |  |  |  |  |  |
| RISK METRICS | -7.87\% | -5.57\% | -4.34\% | -18.33\% | -12.97\% | -10.11\% | -2.81\% | -1.99\% |  | 2.28\% | 4.18\% | 7.22\% | 3.04\% | 6.84\% | 9.89\% |
|  |  |  |  |  |  |  |  |  | $1.55 \%$ |  |  |  |  |  |  |
| HS(100) Long | $-9.74 \%$ | -5.51\% | -3.48\% | -17.17\% | $-8.55 \%$ | $-5.42 \%$ | -2.98\% | $-1.03 \%$ |  | 1.90\% | 5.89\% | 11.22\% |  |  |  |
| position |  |  |  |  |  |  |  |  | 0.77\% |  |  |  |  |  |  |
| HS(250) Long | $-9.53 \%$ | $-5.05 \%$ | -3.31\% | $-10.00 \%$ | $-6.53 \%$ | -4.11\% | -7.48\% | -3.51\% |  | 1.33\% | 5.51\% | 10.84\% |  |  |  |
| position |  |  |  |  |  |  |  |  | $2.42 \%$ |  |  |  |  |  |  |
| HS(FS) Long | -11.02\% | -6.01\% | -3.68\% | -11.16\% | -6.16\% | -3.82\% | -10.84\% | -5.90\% |  | 0.19\% | 4.37\% | 9.32\% |  |  |  |
| position |  |  |  |  |  |  |  |  | 3.59\% |  |  |  |  |  |  |
| HS(100) Short | 15.24\% | 6.42\% | 3.88\% | 7.58\% | 2.90\% | 1.82\% | 23.92\% | 11.09\% | 6.29\% |  |  |  | 1.33\% | 5.13\% | 10.46\% |
| position |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(250) Short | 11.14\% | 5.63\% | 3.31\% | 8.52\% | 3.84\% | 2.17\% | 12.98\% | 6.95\% | 4.72\% |  |  |  | 1.71\% | 5.13\% | 11.60\% |
| position |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(FS) Short | 13.88\% | 6.77\% | 3.86\% | 13.48\% | 6.56\% | 3.78\% | 14.02\% | 7.01\% | 3.99\% |  |  |  | 0.57\% | 3.80\% | 10.27\% |
| position |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Note: Table 11 represents out of sample observations. The number of observations is $526 . *$ denotes each confidence level at $1 \%, 5 \%$ or $10 \%$.

Table 12. Backtesting-TD3-Spot price returns-Long positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1) - N | 0.101 | 1.726 | 9.231*** |  |  | 1.655 |  |  | 10.886*** | 6.733 | 3.819 | 2.653 |
| GARCH (1,1) - T |  |  |  |  |  |  |  |  |  | 10632.244 | 5315.220 | 3227.091 |
| GARCH (1,1) - GED | 19.123*** | 1.204 | $11.390^{* * *}$ |  |  |  |  |  |  | 5.194 | 4.466 | 3.716 |
| $\operatorname{IGARCH}(1,1)-\mathrm{N}$ | 4.814** | 1.204 | 6.473** | 11.439*** | 11.402*** | 25.106*** | 16.253*** | 12.606*** | 31.579*** | 4.530 | 2.634 | 1.885 |
| IGARCH (1,1) - T | 6.402** | 0.113 | 4.253** | 10.295*** | 6.069** | 5.152** | 16.697*** | 6.182** | 9.405*** | 4.908 | 2.850 | 2.021 |
| IGARCH (1,1) - GED | 30.024*** | 0.019 | 9.231*** | 10.477*** | 10.154*** | 8.889*** | 40.501 *** | 10.174*** | 18.120*** | 2.985 | 2.570 | 2.184 |
| (GJR)TGARCH $(1,1)-\mathrm{N}$ | 0.101 | 0.782 | 8.249*** |  |  | 3.130* |  |  | 11.379*** | 6.865 | 3.894 | 2.704 |
| (GJR)TGARCH (1,1) - T |  |  |  |  |  |  |  |  |  | 9674.296 | 4836.135 | 2936.113 |
| (GJR)TGARCH (1,1)- GED | $19.123^{* * *}$ | 1.204 | 12.571*** |  |  | 0.387 |  |  | 12.958*** | 5.116 | 4.400 | 3.662 |
| EGARCH (1,1) - N | 0.013 | 1.204 | 9.231*** |  |  | 8.889*** |  |  | 18.120*** | 6.511 | 3.713 | 2.592 |
| EGARCH (1,1) - T |  |  | 100.705*** |  |  |  |  |  |  | 44.741 | 22.997 | 14.407 |
| EGARCH (1,1) - GED | 21.689*** | 0.454 | 10.277*** |  |  | 0.001 |  |  | 10.278*** | 4.476 | 3.857 | 3.236 |
| APARCH (1,1) - N | 0.332 | 1.726 | 9.231*** |  |  | 3.537* |  |  | 12.768*** | 6.512 | 3.710 | 2.587 |
| APARCH (1,1) - T |  |  |  |  |  |  |  |  |  | 191.026 | 96.193 | 58.885 |
| APARCH (1,1) - GED | $16.671^{* * *}$ | 1.726 | 13.823*** |  |  | 0.288 |  |  | 14.112*** | 4.358 | 3.758 | 3.149 |
| TARCH (1,1) - X - N | 0.013 | 1.204 | 8.249*** |  |  | 3.130* |  |  | 11.379*** | 7.369 | 4.163 | 2.876 |
| TARCH (1,1) - X - T |  |  |  |  |  |  |  |  |  | 8251.111 | 4125.059 | 2504.631 |
| TARCH (1,1) - X - GED | 19.123*** | 0.218 | 15.148*** |  | 0.010 | 0.175 |  | 0.228 | 15.323*** | 5.108 | 4.396 | 3.658 |
| RISK METRICS | 6.402** | 0.782 | 4.936** | 10.295*** | 6.551** | 22.389*** | 16.697*** | 7.332** | 27.325*** | 4.656 | 2.700 | 1.933 |
| HS(100) Long position | 3.412* | 0.838 | 0.836 | 12.727*** | 38.817*** | 54.499*** | 16.140*** | 39.655*** | 55.335*** | 6.749 | 2.581 | 1.446 |
| HS(250) Long position | 0.527 | 0.283 | 0.399 | 9.618*** | 20.802*** | 44.456*** | 10.145*** | 21.084*** | 44.856*** | 5.685 | 2.163 | 1.310 |
| HS(FS) Long position | 5.234** | 0.454 | 0.280 |  | 24.277*** | 45.787*** |  | 24.731*** | 46.067*** | 7.298 | 2.716 | 1.455 |

Note: Table 12 represents out of sample observations. The number of observations is 526 . The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TD3 spot prices for long positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ${ }^{* *}$ and ${ }^{* * *}$ denote significance level at $10 \%, 5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.

Table 13. Backtesting-TD3-Spot price returns-Short positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1) - N | 0.527 | 0.454 | 5.675** |  | 9.613*** | 6.255** |  | 10.067*** | 11.931*** | 6.431 | 3.019 | 1.834 |
|  |  |  |  |  |  |  |  |  |  | 10632.244 | 5315.220 | 3227.091 |
| GARCH (1,1) - GED | 21.689*** | 1.204 | 13.823*** |  | 0.031 | 8.586*** |  | 1.235 | 22.409*** | 4.827 | 3.936 | 2.923 |
| IGARCH (1,1) - N | 10.077*** | 0.838 | 0.957 | 13.875*** | 10.448*** | 24.070*** | 23.952*** | 11.287*** | 25.027*** | 3.992 | 1.830 | 1.098 |
| IGARCH (1,1)- T | 19.123*** | 5.657** | 0.041 | 14.618*** | 10.470*** | 15.072*** | 33.741*** | 16.127*** | 15.113*** | 4.279 | 2.143 | 1.213 |
| $\operatorname{IGARCH}(1,1)-\mathrm{GED}$ | 63.476*** | 7.445*** | 0.055 | 13.180*** | 11.890*** | 14.998*** | 76.655*** | 19.335*** | 15.052*** | 2.375 | 1.740 | 1.343 |
| (GJR)TGARCH $(1,1)-\mathrm{N}$ | 0.527 | 0.782 | 5.675** |  | 10.477*** | 6.255** |  | 11.258*** | 11.931*** | 6.561 | 3.117 | 1.878 |
| (GJR)TGARCH ( 1,1 ) - T | 6.561** | 3.117* | 1.878 |  |  |  |  |  |  | 9674.296 | 4836.135 | 2936.113 |
| (GJR)TGARCH (1,1)-GED | 21.689*** | 0.782 | $12.571^{* * *}$ |  | 0.007 | $7.871 * * *$ |  | 0.789 | 20.442*** | 4.753 | 3.863 | 2.860 |
| EGARCH (1,1) - N | 3.412* | 1.204 | 6.473** | 6.506** | 11.402*** | $6.858^{* * *}$ | 9.918*** | 12.606*** | 13.331*** | 5.800 | 2.966 | 1.776 |
| EGARCH (1,1) - T | 5.234** | 34.644*** | 76.301 *** |  |  |  |  |  |  | 44.548 | 22.774 | 14.135 |
| EGARCH (1,1) - GED | 27.145*** | 0.113 | 10.277*** | 11.402*** | 9.346*** | 6.565** | 38.547*** | 9.460*** | 16.842*** | 3.697 | 3.037 | 2.457 |
| APARCH (1,1) - N | 1.243 | 1.204 | 4.253** | 2.658 | 11.402*** | 7.619*** | 3.901 | $12.606^{* * *}$ | 11.872*** | 6.037 | 2.955 | 1.706 |
| APARCH (1,1) - T |  |  |  |  |  |  |  |  |  | 191.026 | 96.193 | 58.885 |
| APARCH (1,1) - GED | 32.998*** | 0.004 | 16.549*** | 9.613*** | 11.013*** | 10.154*** | 42.611*** | 11.017*** | 26.703*** | 3.547 | 2.960 | 2.416 |
| TARCH (1,1)- X - N | 0.527 | 1.726 | 6.473** |  | 12.396*** | 4.393** |  | 14.122*** | 10.867*** | 7.069 | 3.381 | 2.081 |
| TARCH (1,1) - X - T |  |  |  |  |  |  |  |  |  | 8251.111 | 4125.059 | 2504.631 |
| TARCH (1,1) - X - GED | 16.671*** | 0.782 | $11.390^{* * *}$ |  | 0.007 | 7.198*** |  | 0.789 | 18.587*** | 4.747 | 3.868 | 2.849 |
| RISK METRICS | 14.342*** | 3.394* | 0.008 | 17.218*** | 13.043*** | 20.312*** | 31.559*** | 16.437*** | 20.320*** | 4.076 | 1.928 | 1.105 |
| HS(100) Short position | 0.527 | 0.019 | 0.120 | 9.618*** | 18.640*** | 39.224*** | 10.145*** | 18.659*** | 39.344*** | 6.226 | 1.865 | 0.763 |
| HS(250) Short position | 2.215 | 0.019 | 1.425 | 7.394*** | 18.640*** | 50.305*** | 9.608*** | 18.659*** | 51.730*** | 5.121 | 1.498 | 0.612 |
| HS(FS) Short position | 1.161 | 1.726 | 0.041 |  | 12.396*** | $50.423 * * *$ |  | $14.122 * * *$ | 50.464*** | 6.970 | 2.057 | 0.729 |

Note: Table 13 represents out of sample observations. The number of observations is 526. The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TD3 spot prices for short positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and $* * *$ denote significance level at $10 \%, 5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level

Table 14. Value at Risk Statistics-TD3-One month price returns.

| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| GARCH (1,1) - N | -11.28\% | -7.97\% | -6.21\% | -67.15\% | -47.49\% | -37.01\% | -6.52\% | -4.61\% | - | 1.33\% | 3.04\% | 5.70\% | 1.90\% | 4.56\% | 6.08\% |
| GARCH (1,1)-T | -16.93\% | - | -9.32\% | -74.67\% | -52.77\% | -41.10\% | -9.47\% | -6.70\% | $3.60 \%$ | 0.57\% | 0.95\% | 1.71\% | 0.76\% | 1.90\% | 2.28\% |
|  |  | 11.97\% |  |  |  |  |  |  | 5.21\% |  |  |  |  |  |  |
| GARCH (1,1) - GED | -7.21\% | $-6.59 \%$ | $-5.85 \%$ | -53.63\% | -49.07\% | -43.62\% | $-5.13 \%$ | -4.68\% | - | 3.80\% | 4.37\% | 5.70\% | 4.37\% | 5.51\% | 6.65\% |
|  |  |  |  |  |  |  |  |  | $4.15 \%$ |  |  |  |  |  |  |
| $\operatorname{IGARCH}(1,1)-\mathrm{N}$ | -10.14\% | $-7.17 \%$ | $-5.59 \%$ | -51.07\% | -36.12\% | -28.15\% | $-4.13 \%$ | $-2.92 \%$ |  | 1.71\% | 4.56\% | 7.98\% | 2.66\% | 5.51\% | 8.17\% |
|  |  |  |  |  |  |  |  |  | 2.28\% |  |  |  |  |  |  |
| $\operatorname{IGARCH}(1,1)-\mathrm{T}$ | -10.84\% | -7.66\% | -5.97\% | -34.89\% | -24.66\% | -19.21\% | $-5.13 \%$ | -3.62\% |  | 1.52\% | 3.42\% | 6.08\% | 2.28\% | 4.37\% | 7.03\% |
|  |  |  |  |  |  |  |  |  | $2.82 \%$ |  |  |  |  |  |  |
| IGARCH (1,1)-GED | -8.08\% | $-7.38 \%$ | -6.56\% | $-22.07 \%$ | -20.19\% | -17.95\% | -3.98\% | -3.63\% |  | 2.85\% | 3.61\% | 4.94\% | $3.42 \%$ | 4.37\% | 5.70\% |
|  |  |  |  |  |  |  |  |  | $3.23 \%$ |  |  |  |  |  |  |
| (GJR)TGARCH | -11.20\% | -7.92\% | -6.18\% | -69.11\% | -48.87\% | -38.09\% | -6.46\% | -4.57\% |  | 1.14\% | 3.04\% | 5.70\% | 1.71\% | 4.18\% | 6.27\% |
| $(1,1)-\mathrm{N}$ |  |  |  |  |  |  |  |  | 3.56\% |  |  |  |  |  |  |
| (GJR)TGARCH | -17.00\% | - | -9.36\% | $-71.83 \%$ | -50.76\% | -39.54\% | -9.37\% | -6.62\% | - | 0.57\% | 1.14\% | 2.09\% | 0.76\% | 1.90\% | 2.66\% |
| $(1,1)-\mathrm{T}$ |  | 12.01\% |  |  |  |  |  |  | 5.16\% |  |  |  |  |  |  |
| $\begin{aligned} & \text { (GJR)TGARCH } \\ & (1,1)-\text { GED } \end{aligned}$ | -7.34\% | -6.71\% | $-5.96 \%$ | -54.15\% | -49.54\% | -44.04\% | $-4.54 \%$ | -4.14\% | - | 3.99\% | 4.18\% | 6.27\% | 4.75\% | 5.70\% | 6.46\% |
|  |  |  |  |  |  |  |  |  | 3.68\% |  |  |  |  |  |  |
| EGARCH (1,1)- N | -10.68\% | $-7.56 \%$ | -5.89\% | -57.05\% | -40.34\% | -31.44\% | $-5.84 \%$ | -4.13\% | - | 1.14\% | 3.04\% | 5.32\% | 1.71\% | 4.37\% | 6.08\% |
|  |  |  |  |  |  |  |  |  | $3.22 \%$ |  |  |  |  |  |  |
| EGARCH (1,1)- T | -13.74\% | -9.71\% | $-7.56 \%$ | -41.16\% | -29.09\% | -22.66\% | $-7.25 \%$ | -5.12\% | - | 0.57\% | 1.52\% | 3.80\% | 1.33\% | 2.47\% | 3.61\% |
|  |  |  |  |  |  |  |  |  | 3.99\% |  |  |  |  |  |  |
| EGARCH (1,1)-GED | $-7.01 \%$ | $-6.40 \%$ | $-5.69 \%$ | -8.17\% | -7.48\% | -6.65\% | -4.28\% | -3.92\% | - | 2.85\% | 3.42\% | 4.94\% | 3.23\% | 3.42\% | 5.13\% |
|  |  |  |  |  |  |  |  |  | 3.48\% |  |  |  |  |  |  |
| APARCH (1,1)- N | -10.90\% | -7.71\% | -6.01\% | -61.20\% | -43.28\% | -33.73\% | $-6.28 \%$ | -4.44\% | - | 0.95\% | 3.23\% | 5.70\% | 1.90\% | 4.56\% | 6.46\% |
|  |  |  |  |  |  |  |  |  | 3.46\% |  |  |  |  |  |  |


| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| APARCH (1,1)- T | - | -9.35\% | -7.28\% | -28.55\% | -20.18\% | -15.72\% | -7.10\% | -5.02\% | - | 0.57\% | 1.90\% | 3.61\% | 1.33\% | 2.66\% | 3.99\% |
|  | 13.23\% |  |  |  |  |  |  |  | 3.91\% |  |  |  |  |  |  |
| APARCH (1,1)-GED | -6.63\% | -6.05\% | -5.38\% | -21.50\% | -19.68\% | -17.49\% | -3.37\% | -3.07\% | - | 4.56\% | 4.94\% | 6.65\% | 5.32\% | 6.27\% | 7.22\% |
|  |  |  |  |  |  |  |  |  | 2.72\% |  |  |  |  |  |  |
| TARCH (1,1)-X - N | - | -7.99\% | $-6.23 \%$ | -71.31\% | -50.43\% | -39.30\% | -5.99\% | $-4.23 \%$ | - | 1.14\% | 3.04\% | 5.70\% | 1.71\% | $3.42 \%$ | 6.08\% |
|  | 11.30\% |  |  |  |  |  |  |  | 3.30\% |  |  |  |  |  |  |
| TARCH (1,1)-X - T | - | - | $-9.43 \%$ | -69.88\% | -49.39\% | -38.46\% | -9.79\% | $-6.92 \%$ | - | 0.57\% | 1.14\% | 2.28\% | 0.76\% | 1.71\% | 2.66\% |
|  | 17.14\% | 12.11\% |  |  |  |  |  |  | 5.39\% |  |  |  |  |  |  |
| TARCH (1,1)-X- | -6.92\% | -6.32\% | $-5.62 \%$ | -44.84\% | -41.03\% | -36.47\% | -5.31\% | $-4.83 \%$ | - | 3.23\% | 4.18\% | 5.70\% | 3.80\% | 4.37\% | 7.03\% |
| GED |  |  |  |  |  |  |  |  | 4.30\% |  |  |  |  |  |  |
| RISK METRICS | - | -7.22\% | $-5.62 \%$ | -49.24\% | -34.82\% | -27.14\% | $-4.22 \%$ | -2.98\% | - | 1.71\% | 4.37\% | 7.79\% | 2.66\% | 5.51\% | 7.79\% |
|  | 10.20\% |  |  |  |  |  |  |  | 2.33\% |  |  |  |  |  |  |
| HS(100) Long position | - | -5.78\% | -3.91\% | -61.12\% | $-9.53 \%$ | -5.30\% | -4.76\% | $-2.84 \%$ | - | 1.14\% | 6.46\% | 9.89\% |  |  |  |
|  | 22.36\% |  |  |  |  |  |  |  | 2.07\% |  |  |  |  |  |  |
| HS(250) Long position | - | $-5.22 \%$ | $-3.43 \%$ | -25.24\% | -6.22\% | -4.55\% | -8.66\% | $-3.92 \%$ | - | 0.95\% | 5.51\% | 12.17\% |  |  |  |
|  | 14.60\% |  |  |  |  |  |  |  | 2.25\% |  |  |  |  |  |  |
| HS(FS) Long position | - | $-7.03 \%$ | $-4.56 \%$ | -18.10\% | -7.41\% | -4.68\% | - | -6.78\% | - | 0.38\% | 3.04\% | 7.41\% |  |  |  |
|  | 17.69\% |  |  |  |  |  | 17.17\% |  | 4.47\% |  |  |  |  |  |  |
| HS(100) Short position | 22.07\% | 6.07\% | 4.03\% | 7.23\% | 4.94\% | 2.47\% | 61.12\% | 8.89\% | 5.51\% |  |  |  | 1.33\% | 5.32\% | 11.03\% |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(250) Short position | 11.71\% | 5.37\% | 3.92\% | 8.11\% | 4.32\% | 2.60\% | 15.59\% | 6.06\% | 4.80\% |  |  |  | 1.71\% | 6.08\% | 11.41\% |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(FS) Short position | 14.41\% | 7.27\% | 5.06\% | 14.02\% | 7.08\% | 4.98\% | 14.54\% | 7.41\% | 5.24\% |  |  |  | 0.95\% | 3.23\% | 7.22\% |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

Note: Table 14 represents out of sample observations. The number of observations is 526 . ${ }^{*}$ denotes each confidence level at $1 \%, 5 \%$ or $10 \%$.

Table 15: Backtesting-TD3-One month price returns-Long positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1) - N | 0.527 | 4.907** | 12.571*** |  | 0.446 | 0.051 |  | 5.354* | 12.622*** | 4.569 | 1.522 | 1.126 |
| GARCH (1,1) - T | 1.161 | 26.894*** | 59.319*** |  |  |  |  |  |  | 5.251 | 4.052 | 2.899 |
| GARCH (1,1) - GED | 24.365*** | 0.454 | 12.571*** | 0.074 | 0.000 | 0.051 | $24.439^{* * *}$ | 0.454 | 12.622*** | 5.979 | 0.804 | 0.777 |
| IGARCH (1,1) - N | 2.215 | 0.218 | 2.532 |  | 0.670 | 0.047 |  | 0.888 | 2.579 | 5.378 | 1.536 | 1.120 |
| IGARCH (1,1) - T | 1.243 | 3.086* | 10.277*** |  | 0.217 | 0.561 |  | 3.303 | 10.838*** | 4.093 | 1.204 | 0.950 |
| $\operatorname{IGARCH}(1,1)-\mathrm{GED}$ | $12.141^{* * *}$ | 2.351 | 18.027*** | 0.598 | 0.135 | 0.379 | 12.739*** | 2.486 | 18.406*** | 5.276 | 0.975 | 1.037 |
| (GJR)TGARCH (1,1) - N | 0.101 | 4.907** | 12.571*** |  | 0.446 | 0.387 |  | 5.354* | 12.958*** | 4.721 | 1.586 | 1.174 |
| (GJR)TGARCH (1,1) - T | 1.161 | 23.680*** | 52.327*** |  |  | 1.510 |  |  | $53.837 * * *$ | 5.097 | 3.988 | 2.849 |
| (GJR)TGARCH (1,1) - GED | 27.145*** | 0.782 | 9.231*** | 0.031 | 0.007 | 1.655 | 27.176*** | 0.789 | 10.886*** | 6.116 | 1.026 | 0.962 |
| EGARCH (1,1) - N | 0.101 | 4.907** | 15.148*** |  | 0.446 | 0.203 |  | 5.354* | 15.352*** | 3.571 | 0.805 | 0.690 |
| EGARCH (1,1) - T |  |  | 28.716*** |  | 2.658 | 0.074 |  | 20.878*** | 28.789*** | 2.268 | 1.369 | 1.150 |
| EGARCH (1,1) - GED |  |  | 18.027*** | 0.598 | 0.217 | 0.076 | 12.739*** | 3.303 | 18.104*** | 5.668 | 0.412 | 0.488 |
| APARCH (1,1) - N |  |  | 12.571 *** |  | 0.320 | 0.387 |  | 4.256 | 12.958*** | 4.083 | 1.157 | 0.919 |
| APARCH (1,1)- T |  |  | 30.836*** |  | 1.836 | 0.135 |  | 15.622*** | 30.971 *** | 1.770 | 0.951 | 0.908 |
| APARCH (1,1) - GED |  |  | 7.331*** | 0.010 | 0.076 | 1.083 | 36.073*** | 0.080 | 8.414** | 6.144 | 0.551 | 0.537 |
| TARCH (1,1) - X - N |  |  | 12.571 *** |  | 0.446 | 0.051 |  | 5.354* | 12.622*** | 4.586 | 1.538 | 1.155 |
| TARCH (1,1) - X - T |  |  | 49.119*** |  |  | 1.229 |  |  | $50.348^{* * *}$ | 5.207 | 4.107 | 2.933 |
| TARCH (1,1) - X - GED | 16.671*** | 0.782 | 12.571*** | 0.320 | 0.007 | 0.909 | 16.992*** | 0.789 | 13.480 *** | 5.665 | 0.265 | 0.311 |
| RISK METRICS | 2.215 | 0.454 | 3.052* |  | 0.850 | 0.015 |  | 1.305 | 3.067 | 5.262 | 1.507 | 1.107 |
| HS (100) Long position | 0.101 | 2.181 | 0.008 |  | 1.394 | 3.033* |  | 3.575 | 3.040 | 22.368 | 0.649 | 0.527 |
| HS (250) Long position | 0.013 | 0.283 | 2.586 | 4.578** | 1.118 | 1.558 | 4.592 | 1.400 | 4.144 | 1.117 | 0.553 | 0.551 |
| HS (FS) Long position | 2.672 | 4.907** | 4.253** |  | 0.446 | 1.511 |  | 5.354* | 5.764* | 0.218 | 0.362 | 0.432 |

Table 15 represents out of sample observations. The number of observations is 526 . The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TD3 One month front Forward Freight Agreements prices for long positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%$, $5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.

Table 16. Backtesting-TD3-One month price returns-Short positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1) - N | 3.412* | 0.218 | 10.277*** | 1.836 | 2.563 | 1.942 | 5.249* | 2.780 | 12.219*** | 3.639 | 1.772 | 1.303 |
| GARCH (1,1) - T | 0.332 | 13.786*** | 49.119*** |  | 1.836 | 1.229 |  | 15.622*** | 50.348*** | 5.893 | 4.201 | 2.915 |
| GARCH (1,1) - GED | 32.998*** | 0.283 | 7.331 *** | 0.850 | 1.118 | 1.158 | 33.848*** | 1.400 | 8.488** | 3.947 | 1.119 | 1.008 |
| IGARCH (1,1) - N | 10.077*** | 0.283 | 2.063 | 3.871** | 2.969* | 3.319* | 13.948*** | 3.252 | 5.382* | 4.044 | 1.751 | 1.270 |
| IGARCH (1,1) - T | 6.402** | 0.454 | 5.675** | 1.229 | 5.917** | 6.255** | 7.631** | 6.372** | 11.931*** | 2.864 | 1.327 | 1.036 |
| IGARCH (1,1) - GED | 19.123*** | 0.454 | $12.571^{* * *}$ | 5.419** | 5.917** | 11.296*** | 24.542*** | 6.372** | 23.868*** | 3.259 | 1.076 | 1.081 |
| (GJR)TGARCH $(1,1)-\mathrm{N}$ | 2.215 | 0.782 | 9.231*** | 2.085 | 1.159 | 11.908*** | 4.299 | 1.940 | 21.139*** | 3.695 | 1.785 | 1.302 |
| (GJR)TGARCH (1,1) - T | 0.332 | 13.786*** | 43.203*** |  | 1.836 | 3.871 ** |  | 15.622*** | 47.073*** | 5.798 | 4.175 | 2.892 |
| (GJR)TGARCH (1,1) - GED | 39.215*** | 0.525 | 8.249*** | 0.513 | 2.598 | 1.394 | 39.728*** | 3.123 | 9.643*** | 4.153 | 1.403 | 1.241 |
| EGARCH (1,1) - N | 2.215 | 0.454 | 10.277*** | 2.215 | 2.942* | 0.561 | 4.430 | 3.396 | 10.838*** | 2.408 | 1.021 | 0.830 |
| EGARCH (1,1) - T | 0.527 | 8.631*** | 30.836*** |  | 4.421** | 4.835** |  | 13.052*** | 35.671*** | 1.846 | 1.448 | 1.167 |
| EGARCH (1,1) - GED | 16.671*** | 3.086* | 16.549*** | 2.529 | 2.167 | 0.267 | 19.201*** | 5.254* | 16.815*** | 3.256 | 0.406 | 0.426 |
| APARCH (1,1) - N | 3.412* | 0.218 | 8.249*** | 1.836 | 2.563 | 1.394 | 5.249* | 2.780 | 9.643*** | 2.928 | 1.330 | 1.019 |
| APARCH (1,1) - T | 0.527 | 7.246*** | 26.700*** |  | 3.871** | 3.808* |  | 11.116*** | 30.508*** | 1.104 | 0.951 | 0.844 |
| APARCH (1,1) - GED | 49.164*** | 1.668 | 4.936** | 1.352 | 1.655 | 3.503* | 50.516*** | 3.323 | 8.438** | 3.722 | 0.644 | 0.580 |
| TARCH (1,1) - X - N | 2.215 | 3.086* | 10.277*** | 2.215 | 2.167 | 1.942 | 4.430 | 5.254* | 12.219*** | 3.584 | 1.755 | 1.285 |
| TARCH (1,1)- X - T | 0.332 | 15.890*** | 43.203*** |  | 2.215 | 3.871** |  | 18.105*** | 47.073*** | 5.932 | 4.274 | 2.957 |
| TARCH (1,1)-X - GED | 24.365*** | 0.454 | 5.675** | 1.550 | 0.850 | 0.757 | 25.915*** | 1.305 | 6.432** | 3.601 | 0.653 | 0.612 |
| RISK METRICS | 10.077*** | 0.283 | 3.052* | $3.871^{* *}$ | 2.969* | 4.177** | 13.948*** | 3.252 | 7.229** | 3.935 | 1.712 | 1.249 |
| HS(100) Short position | 0.527 | 0.113 | 0.598 | 9.618*** | 1.352 | 1.212 | 10.145*** | 1.465 | 1.810 | 22.717 | 0.522 | 0.546 |
| HS(250) Short position | 2.215 | 1.220 | 1.112 | 7.394*** | 0.001 | 2.817* | 9.608*** | 1.221 | 3.928 | 0.855 | 0.571 | 0.543 |
| HS(FS) Short position | 0.013 | 3.936** | 4.936** |  | 2.529 | 0.026 |  | 6.465** | 4.961* | 0.234 | 0.362 | 0.427 |

Note: Table 16 represents out of sample observations. The number of observations is 526. The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TD3 One month front Forward Freight Agreements prices for short positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%$, 5\% and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.
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Table 17. Value at Risk Statistics-TD3-three months price returns.

| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| GARCH (1,1) - N | -5.48\% | -3.87\% | -3.02\% | -15.74\% | -11.13\% | -8.67\% | -3.11\% | -2.20\% | - | 2.28\% | 3.23\% | 6.46\% | 1.90\% | 4.56\% | 6.65\% |
|  | -5.84\% | -4.12\% | -3.21\% | -15.19\% | -10.74\% | -8.36\% | -2.61\% | -1.85\% | $1.72 \%$ | 1.90\% | 3.04\% | 5.32\% | 1.90\% | 3.99\% | 6.08\% |
| GARCH (1,1)- T |  |  |  |  |  |  |  |  | 1.44\% |  |  |  |  |  |  |
| GARCH (1,1) - GED | -4.02\% | -3.68\% | -3.27\% | -13.45\% | $-12.32 \%$ | $-10.95 \%$ | -3.04\% | -2.77\% | - | 3.42\% | 4.56\% | 5.70\% | 3.80\% | 4.56\% | 5.70\% |
|  |  |  |  |  |  |  |  |  | 2.46\% |  |  |  |  |  |  |
| $\operatorname{IGARCH}(1,1)-\mathrm{N}$ | -4.60\% | -3.25\% | $-2.53 \%$ | -8.14\% | -5.76\% | -4.49\% | -2.86\% | -2.02\% | - | 2.85\% | 3.99\% | 7.41\% | 2.66\% | 6.46\% | 8.94\% |
|  |  |  |  |  |  |  |  |  | 1.58\% |  |  |  |  |  |  |
| $\operatorname{IGARCH}(1,1)-\mathrm{T}$ | -4.65\% | -3.29\% | $-2.56 \%$ | -8.83\% | -6.24\% | -4.86\% | $-2.71 \%$ | -1.92\% |  | 2.85\% | 3.80\% | 7.79\% | 2.66\% | 6.65\% | 8.94\% |
|  |  |  |  |  |  |  |  |  | 1.49\% |  |  |  |  |  |  |
| $\operatorname{IGARCH}(1,1)-\mathrm{GED}$ | $-3.33 \%$ | -3.04\% | $-2.71 \%$ | -5.54\% | -5.08\% | -4.51\% | -2.18\% | -1.99\% |  | 3.99\% | 4.94\% | 6.84\% | 6.08\% | 7.79\% | 8.56\% |
|  |  |  |  |  |  |  |  |  | 1.77\% |  |  |  |  |  |  |
| (GJR)TGARCH | -5.44\% | -3.85\% | -3.00\% | -14.73\% | -10.42\% | -8.12\% | $-3.04 \%$ | $-2.15 \%$ |  | 2.09\% | 3.42\% | 6.65\% | 1.90\% | 4.56\% | 6.84\% |
| (1,1)-N |  |  |  |  |  |  |  |  | 1.68\% |  |  |  |  |  |  |
| (GJR)TGARCH | - | - | $-9.68 \%$ | -41.75\% | -29.51\% | -22.98\% | -7.61\% | -5.38\% | - | 0.00\% | 0.19\% | 0.19\% | 0.00\% | 0.19\% | 0.57\% |
| (1,1)-T | 17.59\% | 12.43\% |  |  |  |  |  |  | 4.19\% |  |  |  |  |  |  |
| (GJR)TGARCH | -4.05\% | -3.70\% | $-3.29 \%$ | -13.64\% | -12.49\% | -11.11\% | -3.02\% | -2.76\% | - | $3.42 \%$ | 4.56\% | 5.70\% | 3.99\% | 4.75\% | 5.70\% |
| $(1,1)-\text { GED }$ |  |  |  |  |  |  |  |  | 2.45\% |  |  |  |  |  |  |
| EGARCH (1,1) - N | -5.37\% | -3.79\% | -2.96\% | -11.68\% | -8.26\% | -6.44\% | $-2.55 \%$ | -1.80\% | - | 2.28\% | 3.23\% | 6.08\% | 1.90\% | 4.18\% | 7.03\% |
|  |  |  |  |  |  |  |  |  | 1.40\% |  |  |  |  |  |  |
| EGARCH (1,1)- T | - | - | -8.08\% | -37.53\% | -26.52\% | -20.66\% | -5.98\% | -4.22\% | - | 0.00\% | 0.19\% | 0.19\% | 0.00\% | 0.38\% | 0.95\% |
|  | 14.68\% | 10.37\% |  |  |  |  |  |  | $3.29 \%$ |  |  |  |  |  |  |
| $\text { EGARCH }(1,1)-$ | -4.17\% | -3.81\% | $-3.39 \%$ | $-12.53 \%$ | -11.48\% | -10.20\% | -3.18\% | $-2.90 \%$ | - | 3.04\% | 3.80\% | 4.94\% | 3.42\% | 4.37\% | 5.51\% |
| GED |  |  |  |  |  |  |  |  | 2.58\% |  |  |  |  |  |  |
| APARCH (1,1) - N | -5.36\% | -3.79\% | -2.95\% | -11.84\% | -8.37\% | -6.53\% | -2.65\% | -1.87\% | - | 2.28\% | 3.23\% | 6.46\% | 1.90\% | 4.37\% | 7.03\% |
|  |  |  |  |  |  |  |  |  | 1.46\% |  |  |  |  |  |  |


| Model Type | Average Value at Risk |  |  | Minimum Value at Risk |  |  | Maximum Value at Risk |  |  | Hit Sequence Long Position |  |  | Hit Sequence Short Position |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* | 1\%* | 5\%* | 10\%* |
| APARCH (1,1)-T | - | -9.79\% | -7.62\% | -34.77\% | -24.57\% | -19.14\% | -5.69\% | -4.02\% | -3.13\% | 0.00\% | 0.19\% | 0.76\% | 0.19\% | 0.38\% | 0.95\% |
|  | 13.85\% |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| APARCH (1,1)-GED | -3.77\% | -3.44\% | -3.06\% | -13.84\% | -12.68\% | $-11.27 \%$ | $-2.59 \%$ | -2.36\% | -2.10\% | 4.18\% | 5.13\% | 6.65\% | 4.75\% | 5.13\% | 6.84\% |
| TARCH (1,1) - X - N | $-5.45 \%$ | -3.86\% | $-3.01 \%$ | -14.72\% | -10.41\% | -8.11\% | -3.01\% | -2.13\% | $-1.66 \%$ | 2.09\% | 3.42\% | 6.65\% | 1.90\% | 4.56\% | 6.84\% |
| TARCH (1,1)-X-GED | -3.87\% | $-3.54 \%$ | -3.15\% | -9.91\% | -9.08\% | -8.07\% | $-2.55 \%$ | -2.33\% | $-2.07 \%$ | 3.42\% | 4.37\% | 5.70\% | 4.18\% | 5.13\% | 6.27\% |
| RISK METRICS | -4.72\% | $-3.33 \%$ | $-2.60 \%$ | -13.05\% | $-9.23 \%$ | -7.20\% | -1.71\% | -1.21\% | -0.94\% | 2.85\% | 4.75\% | 7.79\% | 3.04\% | 5.70\% | 8.75\% |
| HS(100) Long | -6.45\% | -3.26\% | $-2.16 \%$ | -9.91\% | -5.65\% | -3.08\% | -3.08\% | -1.36\% | -1.22\% | 1.33\% | 6.08\% | 10.27\% |  |  |  |
| position |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| HS(250) Long position | -6.47\% | -2.96\% | $-1.93 \%$ | $-7.67 \%$ | -4.08\% | -2.82\% | -4.88\% | $-2.53 \%$ | $-1.32 \%$ | 1.14\% | 6.27\% | 12.17\% |  |  |  |
| HS(FS) Long position | -9.03\% | -4.51\% | $-2.92 \%$ | -9.36\% | -4.88\% | -3.06\% | $-8.43 \%$ | -4.31\% | $-2.82 \%$ | 0.19\% | 2.66\% | 6.65\% |  |  |  |
| HS(100) Short position | 7.96\% | 3.47\% | 2.38\% | 3.67\% | 2.38\% | 1.32\% | 16.99\% | 7.20\% | 3.45\% |  |  |  | 1.33\% | 5.70\% | 10.27\% |
| HS(250) Short position | 5.94\% | 3.17\% | 2.07\% | 4.83\% | 2.47\% | 1.36\% | 8.62\% | 3.67\% | 2.74\% |  |  |  | 1.33\% | 6.27\% | 11.41\% |
| HS(FS) Short position | 9.02\% | 4.50\% | 2.83\% | 8.59\% | 4.34\% | 2.72\% | 9.18\% | 4.65\% | 2.93\% |  |  |  | 0.57\% | 3.04\% | 7.98\% |

Note: Table 17 represents out of sample observations. The number of observations is 526 . ${ }^{*}$ denotes each confidence level at $1 \%, 5 \%$ or $10 \%$.

Table 18. Backtesting-TD3-three months price returns-Long positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1)- N | 6.402** | 3.936** | 8.249*** |  | 0.320 | 0.022 |  | 4.256 | 8.271** | 0.722 | 0.114 | 0.074 |
| GARCH (1,1) - T | 3.412* | 4.907** | 15.148*** |  | 0.446 | 0.175 |  | 5.354* | 15.323*** | 0.642 | 0.119 | 0.087 |
| GARCH (1,1) - GED | 19.123*** | 0.218 | 12.571*** | 0.217 | 0.010 | 0.387 | 19.340*** | 0.228 | 12.958*** | 1.188 | 0.094 | 0.070 |
| IGARCH (1,1) - N | $12.141^{* * *}$ | 1.204 | 4.253** | 0.598 | 1.289 | 0.004 | 12.739*** | 2.493 | 4.257 | 0.910 | 0.102 | 0.043 |
| IGARCH (1,1) - T | $12.141^{* * *}$ | 1.726 | 3.052* | 0.598 | 0.074 | 0.015 | 12.739*** | 1.799 | 3.067 | 0.901 | 0.104 | 0.046 |
| IGARCH (1,1) - GED | 27.145*** | 0.004 | 6.473** | 1.289 | 0.379 | 0.125 | 28.434*** | 0.383 | 6.598** | 1.488 | 0.122 | 0.036 |
| (GJR)TGARCH $(1,1)-\mathrm{N}$ | 4.814** | 3.086* | $7.331 * * *$ |  | 0.217 | 0.057 |  | 3.303 | 7.388** | 0.724 | 0.109 | 0.070 |
| (GJR)TGARCH $(1,1)-\mathrm{N}$ |  | 45.321*** | 100.705*** |  |  |  |  |  |  | 6.000 | 4.340 | 3.012 |
| (GJR)TGARCH (1,1) - T | 19.123*** | 0.218 | 12.571*** | 0.217 | 0.010 | 0.387 | 19.340*** | 0.228 | 12.958*** | 1.180 | 0.095 | 0.074 |
| (GJR)TGARCH (1,1) - GED | 6.402** | 3.936** | 10.277*** |  | 0.320 | 0.001 |  | 4.256 | 10.278*** | 0.697 | 0.088 | 0.055 |
| EGARCH (1,1) - N |  | 45.321*** | 100.705*** |  |  |  |  |  |  | 3.337 | 2.625 | 1.879 |
| EGARCH (1,1) - GED | 14.342*** | 1.726 | 18.027*** |  | 0.074 | 0.076 |  | 1.799 | 18.104*** | 1.092 | 0.058 | 0.054 |
| APARCH (1,1) - N | 6.402** | 3.936** | 8.249*** |  | 0.320 | 0.022 |  | 4.256 | 8.271** | 0.702 | 0.088 | 0.055 |
| APARCH (1,1) - T |  | $45.321^{* * *}$ | 81.415*** |  |  |  |  |  |  | 2.675 | 2.185 | 1.583 |
| APARCH (1,1) - GED | 30.024*** | 0.019 | 7.331*** | 0.007 | 0.133 | 0.057 | 30.031 *** | 0.152 | 7.388** | 1.316 | 0.126 | 0.076 |
| TARCH (1,1) - X - N | 4.814** | 3.086* | $7.331 * * *$ |  | 0.217 | 0.057 |  | 3.303 | 7.388** | 0.721 | 0.109 | 0.070 |
| TARCH (1,1) - X - T |  |  |  |  |  |  |  |  |  | 2.857 | 0.801 | 0.404 |
| TARCH (1,1) - X - GED | 19.123*** | 0.454 | 12.571*** | 0.217 | 0.000 | 0.051 | 19.340*** | 0.454 | 12.622*** | 1.254 | 0.099 | 0.062 |
| RISK METRICS | $12.141^{* * *}$ | 0.069 | 3.052* | 0.598 | 0.513 | 0.600 | 12.739*** | 0.582 | 3.652 | 0.985 | 0.152 | 0.076 |
| HS(100) Long position | 0.527 | 1.220 | 0.041 |  | 0.561 | 0.044 |  | 1.781 | 0.085 | 0.417 | 0.123 | 0.071 |
| HS(250) Long position | 0.101 | 1.668 | 2.586 |  | 0.003 | 0.110 |  | 1.671 | 2.696 | 0.310 | 0.121 | 0.081 |
| HS(FS) Long position | 5.234** | 7.246*** | 7.331*** |  |  | 0.057 |  |  | 7.388** | 0.010 | 0.010 | 0.020 |

Note: Table 18 represents out of sample observations. The number of observations is 526 . The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TD3 Three months front Forward Freight Agreements prices for long positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and $* * *$ denote significance level at $10 \%$, $5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.
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Table 19. Backtesting-TD3-three months price returns-Short positions.

| Model Type | KUC |  |  | Ch.In. |  |  | J.T. |  |  | Q.L.F. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% | 1\% | 5\% | 10\% |
| GARCH (1,1) - N | 3.412* | 0.218 | $7.331 * * *$ |  | 0.010 | 0.203 |  | 0.228 | 7.534** | 0.822 | 0.130 | 0.092 |
| GARCH $(1,1)-\mathrm{T}$ | 3.412* | 1.204 | 10.277*** |  | 0.031 | 0.561 |  | 1.235 | 10.838*** | 0.729 | 0.134 | 0.106 |
| GARCH (1,1) - GED | 24.365*** | 0.218 | 12.571*** | 0.074 | 0.010 | 0.387 | 24.439*** | 0.228 | 12.958*** | 1.328 | 0.115 | 0.089 |
| IGARCH (1,1) - N | 10.077*** | 2.181 | 0.685 | 0.777 | 0.301 | 0.172 | 10.854*** | 2.482 | 0.856 | 1.044 | 0.131 | 0.069 |
| IGARCH (1,1) - T | 10.077*** | 2.757* | 0.685 | 0.777 | 1.158 | 0.172 | 10.854*** | 3.915 | 0.856 | 1.033 | 0.132 | 0.071 |
| IGARCH (1,1) - GED | 63.476*** | 7.445*** | 1.277 | 0.561 | 1.042 | 0.376 | 64.037*** | 8.487** | 1.653 | 1.621 | 0.153 | 0.061 |
| (GJR)TGARCH $(1,1)-\mathrm{N}$ | 3.412* | 0.218 | 6.473** |  | 0.670 | 0.125 |  | 0.888 | 6.598** | 0.821 | 0.125 | 0.087 |
| (GJR)TGARCH (1,1) - T |  | 45.321*** | 87.040*** |  |  |  |  |  |  | 5.760 | 4.269 | 3.016 |
| (GJR)TGARCH (1,1) - GED | 27.145*** | 0.069 | $12.571^{* * *}$ | 0.031 | 0.035 | 0.387 | 27.176*** | 0.104 | 12.958*** | 1.316 | 0.116 | 0.092 |
| EGARCH (1,1) - N | 3.412* | 0.782 | 5.675** |  | 0.007 | 0.757 |  | 0.789 | $6.432 * *$ | 0.803 | 0.108 | 0.076 |
| EGARCH (1,1) - T |  | 39.457*** | $76.301^{* * *}$ |  |  |  |  | 39.457*** | 76.301*** | 3.177 | 2.574 | 1.883 |
| EGARCH (1,1) - GED | 19.123*** | 0.454 | 13.823*** | 0.217 | 0.000 | 0.104 | 19.340*** | 0.454 | 13.927*** | 1.230 | 0.082 | 0.076 |
| APARCH (1,1) - N | 3.412* | 0.454 | 5.675** |  | 0.000 | 0.757 |  | 0.454 | 6.432** | 0.807 | 0.109 | 0.077 |
| APARCH (1,1) - T | 5.234** | 39.457*** | $76.301 * * *$ |  |  |  | 5.234* | 39.457*** | 76.301 *** | 2.536 | 2.140 | 1.592 |
| APARCH (1,1) - GED | 39.215*** | 0.019 | 6.473** | 0.035 | 0.133 | 1.261 | 39.251 *** | 0.152 | 7.735** | 1.459 | 0.150 | 0.094 |
| TARCH (1,1) - X - N | 3.412* | 0.218 | $6.473^{* *}$ |  | 0.670 | 0.125 |  | 0.888 | 6.598** | 0.818 | 0.125 | 0.088 |
| TARCH (1,1) - X - T |  |  |  |  |  |  |  |  |  | 1.473 | 0.486 | 0.293 |
| TARCH (1,1)-X - GED | 30.024*** | 0.019 | $9.231 * * *$ | 0.007 | 0.267 | 0.420 | $30.031^{* * *}$ | 0.286 | 9.651*** | 1.392 | 0.121 | 0.081 |
| RISK METRICS | 14.342*** | 0.525 | 0.957 |  | 0.051 | 0.342 |  | 0.576 | 1.299 | 1.101 | 0.176 | 0.096 |
| HS(100) Short position | 0.527 | 0.525 | 0.041 |  | 2.598 | 1.212 |  | 3.123 | 1.253 | 0.572 | 0.108 | 0.077 |
| HS(250) Short position | 0.527 | 1.668 | 1.112 |  | 1.655 | 0.795 |  | 3.323 | 1.907 | 0.579 | 0.131 | 0.097 |
| HS(FS) Short position | 1.161 | 4.907** | 2.532 |  | 2.930* | 0.842 |  | 7.838** | 3.374 | 0.009 | 0.031 | 0.051 |

Note: Table 19 represents out of sample observations. The number of observations is 526. The table represents statistical tests of unconditional, independent and conditional coverage of the interval forecasts under each approach and Loss Function scores for the TD3 Three months front Forward Freight Agreements prices for short positions. Where, KUC (Kupiec Unconditional Coverage Test), Ch.In. (Christoffersen Independence Test), J.T. (Joint Test for conditional coverage), Q.L.F. (Quintile Loss Function). *, ** and *** denote significance level at $10 \%$, $5 \%$ and $1 \%$. Critical values for Ch.In. are $9.21,5.99$ and 4.6 for $1 \%, 5 \%, 10 \%$ significance level respectively. Critical values for J.T. are $6.63,3.84$ and 2.7 for $1 \%, 5 \%, 10 \%$ significance level respectively. If value of the likelihood ratio is larger than the critical value, the VaR model is rejected at the significance level.
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