



Research article

Public investment as a growth driver for a commodity-exporting economy: Sizing up the fiscal-monetary involvement

Serhii Shvets*

Department of Modeling and Forecasting of Economic Development, State Agency “Institute for Economics and Forecasting,” National Academy of Sciences of Ukraine, 26, Panasa Myrnoho, Kyiv, 01011, Ukraine

* **Correspondence:** Email: smserg@ukr.net.

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Appendix

Appendix A. Expanded supplementary stuff.

Equation	Definition
$\frac{(C_t^R - hC_{t-1}^R + \phi C_t^G)(C_{t+1}^R - hC_t^R + \phi C_{t+1}^G)}{(C_{t+1}^R - hC_t^R + \phi C_{t+1}^G) - E_t \beta h (C_t^R - hC_{t-1}^R + \phi C_t^G)} = \frac{W_t}{\chi_L L_t^{R\phi} P_t}$	Ricardian Euler equation
$\chi_L L_t^{R\phi} = \left(\frac{i_t + 1}{i_t} \right) \frac{\chi_M W_t}{M_t}$	Ricardian labor supply
$C_t^{NR} + \phi C_t^G = \frac{W_t}{\chi_L L_t^{NR\phi} P_t}$	Non-Ricardian labor supply
$i_t + 1 = E_t \pi_{t+1} (r_{t+1} - \delta + 1)$	Investment-capital trade-off

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Equation	Definition
$\frac{1+i_t}{1+i_t^*} = \frac{s_{t+1}}{s_t}$	Uncovered interest parity
$w_{j,t}^{\circ} = \chi_L \left(\frac{\omega^w}{\omega^w - 1} \right) E_t \sum_{i=0}^{\infty} \left[(\beta \theta^w)^i \left(\frac{C_{j,t+i}^R - hC_{j,t-1+i}^R + \phi C_{j,t+i}^G}{C_{j,t+i}^R - hC_{j,t+i}^R + \phi C_{j,t+i}^G - \beta h(C_{j,t+i}^R - hC_{j,t-1+i}^R + \phi C_{j,t+i}^G)} \right) L_{j,t+i}^{R\phi} P_{t+i} \right]$	Ricardian optimal wage level
$w_{j,t}^{\circ} = \chi_L \left(\frac{\omega^w}{\omega^w - 1} \right) E_t \sum_{i=0}^{\infty} \left[(\beta \theta^w)^i (C_{j,t+i}^{NR} + \phi C_{j,t+i}^G) L_{j,t+i}^{NR\phi} P_{t+i} \right]$	Non-Ricardian optimal wage level
$W_t = \left[\theta^w W_{t-1}^{1-\omega^w} + (1-\theta^w) W_t^{\circ 1-\omega^w} \right]^{\frac{1}{1-\omega^w}}$	Aggregate wage
Commodity goods sector	
$MC_t^z = \frac{1}{K_{t-1}^g \alpha_g^z} \left(\frac{W_t / P_t^z}{1 - \alpha_k^z} \right)^{1-\alpha_k^z} \left(\frac{r_t}{\alpha_k^z} \right)^{\alpha_k^z}$	Marginal cost
$P_t^z = \left(\frac{\omega^z}{\omega^z - 1} \right) E_t \sum_{n=0}^{\infty} (\beta \theta^z)^n MC_{t+n}^z$	Optimal price level
$P_t^z = \left[\theta^z P_{t-1}^{1-\omega^z} + (1-\theta^z) P_t^{\circ 1-\omega^z} \right]^{\frac{1}{1-\omega^z}}$	Aggregate price level
Final goods sector	
$MC_t^f = \frac{1}{K_{t-1}^g \alpha_g^f} \left(\frac{W_t / P_t^f}{1 - \alpha_k^f - \alpha_z^f} \right)^{1-\alpha_k^f - \alpha_z^f} \left(\frac{r_t}{\alpha_k^f} \right)^{\alpha_k^f}$	Marginal cost
$P_t^f = \left(\frac{\omega^f}{\omega^f - 1} \right) E_t \sum_{n=0}^{\infty} (\beta \theta^f)^n MC_{t+n}^f$	Optimal price level
$P_t^f = \left[\theta^f P_{t-1}^{1-\omega^f} + (1-\theta^f) P_t^{\circ 1-\omega^f} \right]^{\frac{1}{1-\omega^f}}$	Aggregate price level

Source: Obtained using some mathematics about micro-conceptions in detail.

Appendix B. Baseline calibration.

Parameter	Description	Value	Source
β	Subjective discount factor	0.9828	annualized real interest rate is 7%
h	Degree of private consumer's habit formation	0.7	Medina and Soto (2016)
ϕ	Elasticity of substitution between private and government consumption	0.3	normal value
χ_M	Steady-state utility of real money holdings	0.4	normal value
χ_L	Steady-state disutility of labor supply	0.3	normal value
φ	Inverse of the Frisch elasticity of labor supply	2	normal value
δ	Depreciation rate	0.025	normal value
α_k^z	Capital income share in commodity goods production	0.28	Kitano and Takaku (2021)
α_k^f	Capital income share in final goods production	1/3	Kitano and Takaku (2021)
α_z^f	Commodity inputs share in final goods production	0.05	Kitano and Takaku (2021)
α_g^z	Output elasticity of productive government spending in commodity goods production	0.15	Melina et al. (2016)
α_g^f	Output elasticity of productive government spending in final goods production	0.16	Melina et al. (2016)
ε^0	Marginal efficiency of public investment	0.5	Agenor (2016), Melina et al. (2016)
ε^1	Exceeding adjustment costs of public investment	0.1	Agenor (2016)
ω^w	Elasticity of substitution between differentiated labors	20	normal value
ω^z	Elasticity of substitution between wholesale commodity goods	6	normal value
ω^f	Elasticity of substitution between wholesale final goods	6	normal value
ζ^{z*}	Price elasticity of foreign demand for commodity goods	8	normal value
ζ^{f*}	Price elasticity of foreign demand for final goods	8	normal value
θ^w	Degree of nominal wage stickiness	0.75	normal value
θ^z	Degree of price stickiness in commodity goods production	0.75	normal value
θ^f	Degree of price stickiness in final goods production	0.75	normal value
η	Share of rule-of-thumb consumers	0.6	Melina et al. (2016)
Policy parameters			
τ^{z*}	Tax rate on exported raw materials	0.05	author's decision
σ	Share of tax-financed public investment	0.1	Zeyneloglu (2018)
k	Allocation of public spending in favor of investment	1.2	Zeyneloglu (2018)
ρ_i	Persistence of interest rate	0.6	normal value
ρ_π	Response of interest rate to inflation	1.5	normal value
ρ_Y	Response of interest rate to total output	0.1	normal value
ρ_B	Response of interest rate to total public debt-to-output ratio	0.02	author's decision
ρ_{B^*}	Elasticity of the international external premium on public debt in foreign currency	0.01	Drechsel and Tenreyro (2018)
ρ_{Pz^*}	Elasticity of the international external premium to external commodity prices	-0.02	Drechsel and Tenreyro (2018)
Steady-state parameters			
v	Initial public investment share of public spending	0.08	average observed data for developing economies
B^{tot}/Y	Initial total public debt-to-output ratio	0.8	average observed data for developing economies
Violation parameters			
κ^{Pz^*}	Degree of autoregressive foreign commodity price shock	0.9	normal value
κ^g	Degree of autoregressive public spending shock	0.9	normal value

Source: Author's decision unless otherwise stated.

Appendix C. Log-linearization of the model structure.

Equation	Definition
$\bar{C}^R \tilde{C}_t^R + \bar{K}^P \left[\tilde{K}_t^P - \tilde{K}_{t-1}^P (\bar{r} + 1 - \delta) - \bar{r} \tilde{r}_t \right] + \bar{M} (\tilde{M}_t - \tilde{M}_{t-1}) + \bar{B} \left[\tilde{B}_t - \tilde{B}_{t-1} (1 + \bar{i}) - \bar{i} (\tilde{i}_{t-1} - \tilde{P}_t) \right] + \bar{B}^* \left[\tilde{B}_t^* - \tilde{B}_{t-1}^* (1 + \bar{i}^*) - \bar{i}^* (\tilde{s}_t + \tilde{i}_{t-1}^* - \tilde{P}_t) \right] = \bar{W} L^R (\tilde{W}_t + \tilde{L}_t^R - \tilde{P}_t) - \bar{T} \tilde{T}_t$	Ricardian budget constraint
$\tilde{C}_t^{NR} = \tilde{L}_t^{NR} + \tilde{W}_t - \tilde{P}_t$	Non-Ricardian budget constraint
$\bar{C}^R (\tilde{C}_{t+1}^R - h \tilde{C}_t^R) + \phi \bar{C}^g \tilde{C}_{t+1}^g - \beta h (\bar{C}^R (\tilde{C}_t^R - h \tilde{C}_{t-1}^R) + \phi \bar{C}^g \tilde{C}_t^g) = (1 - \beta h) (\bar{C}^R (1 - h) + \phi \bar{C}^g) (\phi \tilde{L}_t^R - (\tilde{W}_t - \tilde{P}_t))$	Ricardian Euler equation
$\bar{C}^{NR} (\tilde{C}_t^{NR} + \phi \tilde{L}_t^{NR}) + \phi \bar{C}^g (\tilde{C}_t^g + \phi \tilde{L}_t^{NR}) = \frac{\bar{W}}{\chi_L \bar{L}^{NR \phi}} (\tilde{W}_t - \tilde{P}_t)$	Non-Ricardian labor supply
$\phi \tilde{L}_t^R = \tilde{W}_t - \tilde{M}_t - \frac{1}{\bar{i} + 1} \tilde{i}$	Ricardian labor supply
$\bar{i} \tilde{i} = \bar{r} \tilde{r}_{t+1} + (\bar{r} - \delta + 1) \tilde{\pi}_{t+1}$	Investment-capital tradeoff
$\tilde{i} - \tilde{i}^* = \tilde{s}_{t+1} - \tilde{s}_t$	Uncovered interest parity
$\tilde{K}_t^P = (1 - \delta) \tilde{K}_{t-1}^P + \delta \tilde{I}^P$	Law motion of private capital
$\tilde{\pi}_t^w = \beta^w \tilde{\pi}_{t+1}^w + \frac{(1 - \theta^w)(1 - \beta \theta^w)}{\theta^w} \left[\frac{1}{(1 - \beta h)(\bar{C}^R (1 - h) + \phi \bar{C}^g)} \left((1 - \beta h) \left(\bar{C}^R (\tilde{C}_t^R + \tilde{C}_{t+1}^R) - h \bar{C}^R (\tilde{C}_{t-1}^R + \tilde{C}_t^R) \right) + \phi \bar{C}^g (\tilde{C}_t^g + \tilde{C}_{t+1}^g) \right) - \left(\bar{C}^R (\tilde{C}_{t+1}^R - \beta h \tilde{C}_t^R) + h \bar{C}^R (\tilde{C}_t^R - \beta h \tilde{C}_{t-1}^R) - \phi \bar{C}^g (\tilde{C}_{t+1}^g - \beta h \tilde{C}_t^g) \right) \right] + \phi \tilde{L}_t^R - (\tilde{W}_t - \tilde{P}_t) \right]$	Ricardian Phillips equation for wage
$\tilde{\pi}_t^w = \beta^w \tilde{\pi}_{t+1}^w + \frac{(1 - \theta^w)(1 - \beta \theta^w)}{\theta^w} \left[\frac{\bar{C}^{NR} \tilde{C}_t^{NR} + \phi \bar{C}^g \tilde{C}_t^g}{\bar{C}^{NR} + \phi \bar{C}^g} + \phi \tilde{L}_t^{NR} - (\tilde{W}_t - \tilde{P}_t) \right]$	Non-Ricardian Phillips equation for wage
$\tilde{\pi}_t^w = \tilde{W}_t - \tilde{W}_{t-1}$	Wage inflation
$\tilde{Y}_t^z = \alpha_k^z \tilde{K}_{t-1}^z + (1 - \alpha_k^z) \tilde{L}_t^z + \alpha_g^z \tilde{K}_{t-1}^g$	Production function for the commodity goods sector
$\tilde{L}_t^z = \tilde{M} C_t^z + \tilde{Y}_t^z - \tilde{W}_t + \tilde{P}_t^z$	Demand for labor in the commodity goods sector
$\tilde{K}_{t-1}^z = \tilde{M} C_t^z + \tilde{Y}_t^z - \tilde{r}_t$	Demand for capital in the commodity goods sector
$\tilde{M} C_t^z = (1 - \alpha_k^z) (\tilde{W}_t - \tilde{P}_t^z) + \alpha_k^z \tilde{r}_t - \alpha_g^z \tilde{K}_{t-1}^g$	Marginal cost in the commodity goods sector
$\tilde{\pi}_t^z = \beta E_t \tilde{\pi}_{t+1}^z + \left[\frac{(1 - \theta^z)(1 - \beta \theta^z)}{\theta^z} \right] (\tilde{M} C_t^z - \tilde{P}_t^z)$	Phillips equation in the commodity goods sector
$\tilde{Y}_t^f = \alpha_k^f \tilde{K}_{t-1}^f + \alpha_z^f \tilde{Z}_t + (1 - \alpha_k^f - \alpha_z^f) \tilde{L}_t^f + \alpha_g^f \tilde{K}_{t-1}^g$	Production function for the final goods sector
$\tilde{L}_t^f = \tilde{M} C_t^f + \tilde{Y}_t^f - \tilde{W}_t + \tilde{P}_t^f$	Demand for labor in the final goods sector
$\tilde{K}_{t-1}^f = \tilde{M} C_t^f + \tilde{Y}_t^f - \tilde{r}_t$	Demand for capital in the final goods sector

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Equation	Definition
$\tilde{MC}_t^f = (1 - \alpha_k^f - \alpha_z^f)(\tilde{W}_t - \tilde{P}_t^f) + \alpha_k^f \tilde{r}_t - \alpha_g^f \tilde{K}_{t-1}^g$	Marginal cost in the final goods sector
$\tilde{\pi}_t^f = \beta E_t \tilde{\pi}_{t+1}^f + \left[\frac{(1 - \theta^f)(1 - \beta\theta^f)}{\theta^f} \right] (\tilde{MC}_t^f - \tilde{P}_t^f)$	Phillips equation in the final goods sector
$\tilde{\pi}_{t+1} = \tilde{P}_{t+1} - \tilde{P}_t$	Gross inflation rate
$\tilde{\pi}_t^z = \tilde{P}_t^z - \tilde{P}_{t-1}^z$	Inflation in the commodity goods sector
$\tilde{\pi}_t^f = \tilde{P}_t^f - \tilde{P}_{t-1}^f$	Inflation in the final goods sector
$\tilde{T}_t^{z*} = \tilde{P}_t^{z*} + \tilde{Y}_t^{z*}$	Tax on exported raw materials
$\bar{B}[\tilde{B}_t - \tilde{B}_{t-1}(1 + \bar{i}) - \bar{i}(\tilde{i}_{t-1} - \tilde{P}_t)] + \bar{B}^*[\tilde{B}_t^* - \tilde{B}_{t-1}^*(1 + \bar{i}^*) - \bar{i}^*(\tilde{s}_t + \tilde{i}_{t-1}^* - \tilde{P}_t)] + \bar{M}(\tilde{M}_t - \tilde{M}_{t-1}) + \bar{T}\tilde{T}_t + \bar{T}^{z*}(\tilde{s}_t + \tilde{T}_t^{z*} - \tilde{P}_t) = \bar{G}\tilde{G}_t + \bar{F}^*[\tilde{F}_t^* - \tilde{F}_{t-1}^*(1 + \bar{i}^*) - \bar{i}^*(\tilde{s}_t + \tilde{i}_{t-1}^* - \tilde{P}_t)]$	Government budget constraint
$\tilde{M}_t = \tilde{B}_t + \frac{\bar{B}}{\bar{Y}}(\tilde{B}_t - \tilde{P}_t)$	Money supply
$\bar{T}\tilde{T}_t + \bar{i}^*\bar{F}^*[\tilde{F}_{t-1}^* + \tilde{s}_t + \tilde{i}_{t-1}^* - \tilde{P}_t] = \sigma\bar{I}^g\tilde{I}_t^g + \bar{C}^g\tilde{C}_t^g + \bar{i}\bar{B}(\tilde{i}_{t-1} + \tilde{B}_{t-1} - \tilde{P}_t) + \bar{i}^*\bar{B}^*(\tilde{s}_t + \tilde{i}_{t-1}^* + \tilde{B}_{t-1}^* - \tilde{P}_t)$	Government revenues
$\tilde{K}_t^g = \tilde{K}_{t-1}^g(1 - \delta + \varepsilon^l\delta) + \delta(\tilde{I}_t^g - \varepsilon^l\tilde{I}_{t-1}^g)$	Law motion of public capital
$\tilde{I}_t^g = \tilde{G}_t$	Public investment
$\tilde{C}_t^g = \tilde{G}_t$	Public consumption
$\bar{G}\tilde{G}_t = \bar{C}^g\tilde{C}_t^g + \bar{I}^g\tilde{I}_t^g$	Public spending
$\bar{F}^*\tilde{F}_t^* = 0$	Law motion of the SWFs
$\tilde{s}_t = \tilde{P}_t^z - \tilde{P}_t^{z*}, \tilde{s}_t = \tilde{P}_t^f - \tilde{P}_t^{f*}$	Nominal exchange rate
$\bar{i}^*\tilde{i}_t^* = \tilde{s}_{t+1} - \tilde{s}_t + \rho_{B^*}\bar{B}^*\tilde{B}_t^* + \rho_{p^{z*}}\tilde{P}_t^{z*}$	Foreign interest rate
$\bar{i}^n(\tilde{i}_t^n - \tilde{i}_t) = \tilde{\pi}_t$	Nominal interest rate
$\bar{i}^n\tilde{i}_t^n = \rho_{i_n}\bar{i}_n\tilde{i}_{t-1}^n + \rho_{\pi}\bar{\pi}\tilde{\pi}_{t-1} + \rho_Y\bar{Y}\tilde{Y}_{t-1} + \rho_s\tilde{s}_{t-1} + \rho_b\frac{\bar{B}(\tilde{B}_{t-1} - \tilde{P}_t) + \bar{B}^*(\tilde{s}_{t-1} + \tilde{B}_{t-1}^* - \tilde{P}_t)}{\bar{Y}}$	Taylor rule
$\bar{Y}\tilde{Y}_t = \bar{C}^p\tilde{C}_t^p + \bar{I}^p\tilde{I}_t^p + \bar{G}\tilde{G}_t + \bar{N}\bar{X}\tilde{N}\tilde{X}_t$	Equilibrium condition
$\tilde{Y}_t^{z*} = \tilde{Y}_t^* + \zeta^{z*}(\tilde{P}_t^* - \tilde{P}_t^{z*})$	Foreign demand for commodity goods
$\tilde{Y}_t^{f*} = \tilde{Y}_t^* + \zeta^{f*}(\tilde{P}_t^* - \tilde{P}_t^{f*})$	Foreign demand for final goods
$\bar{Y}^*\tilde{Y}_t^* = 0$	Foreign output
$\bar{N}\bar{X}\tilde{N}\tilde{X}_t = \bar{Y}^{z*}(\tilde{Y}_t^{z*} + \tilde{P}_t^{z*} - \tilde{P}_t^*) + \bar{Y}^{f*}(\tilde{Y}_t^{f*} + \tilde{P}_t^{f*} - \tilde{P}_t^*)$	Foreign trade balance
$\bar{N}\bar{X}(\tilde{N}\tilde{X}_t + \tilde{P}^*) + \bar{B}^*(\tilde{B}_t^* - \tilde{B}_{t-1}^*) - \bar{i}^*\bar{B}^*(\tilde{i}_{t-1}^* + \tilde{B}_{t-1}^*) + \bar{T}^{z*}\tilde{T}_t^{z*} = \bar{F}^*(\tilde{F}_t^* - \tilde{F}_{t-1}^*) - \bar{i}^*\bar{F}^*(\tilde{i}_{t-1}^* + \tilde{F}_{t-1}^*)$	External account
$\bar{Y}\tilde{Y}_t = \bar{Y}^f(\tilde{Y}_t^f + \tilde{P}_t^f - \tilde{P}_t) + \bar{Y}^z(\tilde{Y}_t^z + \tilde{P}_t^z - \tilde{P}_t) - \bar{Z}(\tilde{Z}_t + \tilde{P}_t^z - \tilde{P}_t)$	All goods production

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Equation	Definition
$\tilde{K}_t^p = \frac{\tilde{K}_t^z + \tilde{K}_t^f}{2}$	Aggregate private capital
$\frac{\tilde{L}_t^z + \tilde{L}_t^f}{2} = (1-\eta)\tilde{L}_t^R + \eta\tilde{L}_t^{NR}$	Aggregate labor
$\tilde{C}_t^p = (1-\eta)\tilde{C}_t^R + \eta\tilde{C}_t^{NR}$	Aggregate consumption
$\overline{BYBY}_t = \frac{\overline{B}}{\overline{Y}}(\tilde{B}_t - \tilde{Y}_t - \tilde{P}_t) + \frac{\overline{B}^*}{\overline{Y}}(\tilde{s}_t + \tilde{B}_t^* - \tilde{Y}_t - \tilde{P}_t)$	Total debt ratio
$\tilde{P}_t^{z*} = \kappa^{p^{z*}} \tilde{P}_{t-1}^{z*} + \tilde{v}_t / 10$	Foreign commodity price shock
$\tilde{G}_t = \kappa^g \tilde{G}_{t-1} + \tilde{v}_t$	Public spending shock

Source: Product of author's derivation.



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