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*Research article*

## **Reduction of carbon emissions under sustainable supply chain management with uncertain human learning**

**Richi Singh<sup>1</sup>, Dharmendra Yadav<sup>2</sup>, S.R. Singh<sup>3</sup>, Ashok Kumar<sup>4</sup> and Biswajit Sarkar<sup>5,\*</sup>**

<sup>1</sup> Department of Mathematics, Meerut College, Meerut (UP) India

<sup>2</sup> Department of Mathematics, Vardhaman College, Bijnor (UP) India

<sup>3</sup> Department of Mathematics, CCS University, Meerut (UP) India

<sup>4</sup> Department of Mathematics, Meerut College, Meerut (UP) India

<sup>5</sup> Department of Industrial Engineering, Yonsei University, 50 Yonsei-ro, Sinchon-dong, Seodaemun-gu, Seoul, South Korea

\***Correspondence:** [bsbiswajitsarkar@gmail.com](mailto:bsbiswajitsarkar@gmail.com); Tel: +821074981981.

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### **Appendix 1**

Inventory holding cost for the manufacturer in each production cycle will be

$$H_M \int_{t_0}^T I_M(t) dt = \frac{H_M P (T - t_0)^2}{2}$$

$$\text{Manufacturing cost} = C_M P (T - t_0)$$

$$\text{Setup cost of manufacturer} = C_{OM}$$

$$\text{Screening cost} = C_{SM} P (T - t_0)$$

$$\text{Waste disposal cost} = C_W P_3 P (T - t_0)$$

$$\text{Total cost of transportation} = \sum_{i=1}^n C_{TM_i} P_1 P (T - t_0) + C_{TA} P_2 P (T - t_0)$$

### **Appendix 2**

Shortage cost of the  $i^{th}$  retailer

$$= C_{B_i} \int_{T_2}^{2T} (-I_{R_{i3}}(t)) dt = \frac{C_{B_i}}{2} \left( \frac{S_i^2}{B_i D_i} \right)$$

Lost sale cost of the  $i^{th}$  retailer

$$= C_{Li} \int_{T_2}^{2T} (1 - B_i) D_i dt = C_{Li} (1 - B_i) \left( \frac{S_i}{B_i} \right)$$

Holding cost of the  $i^{th}$  retailer

$$\begin{aligned} &= H_{Ri} \left( \int_T^{T_1} I_{Ri1}(t) dt + \int_{T_1}^{T_2} I_{Ri2}(t) dt \right) + H_{WRi} \left( \frac{(Q_i)^2 p_i(m)}{x_i} \right) \\ &= H_{Ri} \left[ \frac{(Q_i)^2 (1 - p_i(m))^2}{2D_i \log \left( \frac{1 + l_i + k_i(\epsilon) - T}{1 + l_i + k_i(\epsilon) - 2T + \frac{S_i}{B_i D_i}} \right)} + \frac{D_i}{4} \left( \left( 1 + l_i + k_i(\epsilon) - 2T + \frac{S_i}{B_i D_i} \right)^2 - (1 + l_i + k_i(\epsilon) - T)^2 \right) \right] + \\ &\frac{Q_i}{2(1 + l_i + k_i(\epsilon) - T)} \left( \frac{(Q_i)^2 (1 - p_i(m))^2}{D_i \log \left( \frac{1 + l_i + k_i(\epsilon) - T}{1 + l_i + k_i(\epsilon) - 2T + \frac{S_i}{B_i D_i}} \right)^2} - (1 + l_i + k_i(\epsilon) - T)^2 \right) + H_{WRi} \left( \frac{(Q_i)^2 p_i(m)}{x_i} \right) \end{aligned}$$

Cost of screening of product for the  $i^{th}$  retailer =  $C_{SRi} Q_i$

Cost of placing an order for the  $i^{th}$  retailer =  $C_{ORi}$

Wholesale purchasing price of the  $i^{th}$  retailer =  $w_i Q_i$

Advertisement cost for the  $i^{th}$  retailer =  $NC_{Ai}$

Preservation technology cost =  $\epsilon T$

Deterioration cost of the  $i^{th}$  retailer

$$\begin{aligned} &= H_{DRi} \left[ \int_T^{T_1} \left( \frac{1}{1 + l_i + k_i(\epsilon) - t} \right) (D_i (1 + l_i + k_i(\epsilon) - t) \log \left( \frac{1 + l_i + k_i(\epsilon) - t}{1 + l_i + k_i(\epsilon) - T} \right) \right. \\ &\quad \left. + \left( \frac{1 + l_i + k_i(\epsilon) - t}{1 + l_i + k_i(\epsilon) - T} \right) Q_i) dt \right. \\ &\quad \left. + \int_{T_1}^{T_2} \left( \frac{1}{1 + l_i + k_i(\epsilon) - t} \right) (D_i (1 + l_i + k_i(\epsilon) - t) \log \left( \frac{1 + l_i + k_i(\epsilon) - t}{1 + l_i + k_i(\epsilon) - 2T + \frac{S_i}{B_i D_i}} \right) \right) dt \right] \\ &= H_{DRi} \left[ Q_i - \frac{(Q_i)^2 (1 - p_i(m))}{D_i (1 + l_i + k_i(\epsilon) - T) \log \left( \frac{1 + l_i + k_i(\epsilon) - T}{1 + l_i + k_i(\epsilon) - 2T + \frac{S_i}{B_i D_i}} \right)} - D_i \left( T - \frac{S_i}{B_i D_i} \right) + Q_i (1 \right. \\ &\quad \left. - p_i(m)) \right] \end{aligned}$$

### Appendix 3

$$\widetilde{C}_M = (C_M - \Delta_{C_M}^l, C_M, C_M - \Delta_{C_M}^u), 0 < \Delta_{C_M}^l < C_M \text{ and } 0 < \Delta_{C_M}^u$$

$$\begin{aligned}
\widetilde{C}_W &= (C_W - \Delta_{C_W}^l, C_W, C_W - \Delta_{C_W}^u), 0 < \Delta_{C_W}^l < C_W \text{ and } 0 < \Delta_{C_W}^u \\
\widetilde{C}_{OM} &= (C_{OM} - \Delta_{C_{OM}}^l, C_{OM}, C_{OM} - \Delta_{C_{OM}}^u), 0 < \Delta_{C_{OM}}^l < C_{OM} \text{ and } 0 < \Delta_{C_{OM}}^u \\
\widetilde{C}_{SM} &= (C_{SM} - \Delta_{C_{SM}}^l, C_{SM}, C_{SM} - \Delta_{C_{SM}}^u), 0 < \Delta_{C_{SM}}^l < C_{SM} \text{ and } 0 < \Delta_{C_{SM}}^u \\
\widetilde{C}_{TA} &= (C_{TA} - \Delta_{C_{TA}}^l, C_{TA}, C_{TA} - \Delta_{C_{TA}}^u), 0 < \Delta_{C_{TA}}^l < C_{TA} \text{ and } 0 < \Delta_{C_{TA}}^u \\
\widetilde{C}_{PA} &= (C_{PA} - \Delta_{C_{PA}}^l, C_{PA}, C_{PA} - \Delta_{C_{PA}}^u), 0 < \Delta_{C_{PA}}^l < C_{PA} \text{ and } 0 < \Delta_{C_{PA}}^u \\
\widetilde{C}_{TM_i} &= (C_{TM_i} - \Delta_{C_{TM_i}}^l, C_{TM_i}, C_{TM_i} - \Delta_{C_{TM_i}}^u), 0 < \Delta_{C_{TM_i}}^l < C_{TM_i} \text{ and } 0 < \Delta_{C_{TM_i}}^u \\
\widetilde{C}_{OR_i} &= (C_{OR_i} - \Delta_{C_{OR_i}}^l, C_{OR_i}, C_{OR_i} - \Delta_{C_{OR_i}}^u), 0 < \Delta_{C_{OR_i}}^l < C_{OR_i} \text{ and } 0 < \Delta_{C_{OR_i}}^u \\
\widetilde{C}_{SR_i} &= (C_{SR_i} - \Delta_{C_{SR_i}}^l, C_{SR_i}, C_{SR_i} - \Delta_{C_{SR_i}}^u), 0 < \Delta_{C_{SR_i}}^l < C_{SR_i} \text{ and } 0 < \Delta_{C_{SR_i}}^u \\
\widetilde{C}_{B_i} &= (C_{B_i} - \Delta_{C_{B_i}}^l, C_{B_i}, C_{B_i} - \Delta_{C_{B_i}}^u), 0 < \Delta_{C_{B_i}}^l < C_{B_i} \text{ and } 0 < \Delta_{C_{B_i}}^u \\
\widetilde{C}_{L_i} &= (C_{L_i} - \Delta_{C_{L_i}}^l, C_{L_i}, C_{L_i} - \Delta_{C_{L_i}}^u), 0 < \Delta_{C_{L_i}}^l < C_{L_i} \text{ and } 0 < \Delta_{C_{L_i}}^u \\
\widetilde{H}_M &= (H_M - \Delta_{H_M}^l, H_M, H_M - \Delta_{H_M}^u), 0 < \Delta_{H_M}^l < H_M \text{ and } 0 < \Delta_{H_M}^u \\
\widetilde{H}_{R_i} &= (H_{R_i} - \Delta_{H_{R_i}}^l, H_{R_i}, H_{R_i} - \Delta_{H_{R_i}}^u), 0 < \Delta_{H_{R_i}}^l < H_{R_i} \text{ and } 0 < \Delta_{H_{R_i}}^u \\
\widetilde{H}_{WR_i} &= (H_{WR_i} - \Delta_{H_{WR_i}}^l, H_{WR_i}, H_{WR_i} - \Delta_{H_{WR_i}}^u), 0 < \Delta_{H_{WR_i}}^l < H_{WR_i} \text{ and } 0 < \Delta_{H_{WR_i}}^u \\
\widetilde{H}_{DR_i} &= (H_{DR_i} - \Delta_{H_{DR_i}}^l, H_{DR_i}, H_{DR_i} - \Delta_{H_{DR_i}}^u), 0 < \Delta_{H_{DR_i}}^l < H_{DR_i} \text{ and } 0 < \Delta_{H_{DR_i}}^u \\
\widetilde{\epsilon} &= (\epsilon - \Delta_{\epsilon}^l, \epsilon, \epsilon - \Delta_{\epsilon}^u), 0 < \Delta_{\epsilon}^l < \epsilon \text{ and } 0 < \Delta_{\epsilon}^u
\end{aligned}$$

#### Appendix 4

$$d(\widetilde{C}_M, \bar{0}) = \frac{(C_M - \Delta_{C_M}^l) + 2C_M + (C_M + \Delta_{C_M}^u)}{4} = C_M + \frac{(\Delta_{C_M}^u - \Delta_{C_M}^l)}{4},$$

$$\Delta_{C_M}^l > 0 \text{ and } \Delta_{C_M}^u > 0$$

Similarly,

$$\begin{aligned}
d(\widetilde{C}_W, \bar{0}) &= C_W + \frac{(\Delta_{C_W}^u - \Delta_{C_W}^l)}{4}, \Delta_{C_W}^l > 0 \text{ and } \Delta_{C_W}^u > 0 \\
d(\widetilde{C}_{OM}, \bar{0}) &= C_{OM} + \frac{(\Delta_{C_{OM}}^u - \Delta_{C_{OM}}^l)}{4}, \Delta_{C_{OM}}^l > 0 \text{ and } \Delta_{C_{OM}}^u > 0 \\
d(\widetilde{C}_{SM}, \bar{0}) &= C_{SM} + \frac{(\Delta_{C_{SM}}^u - \Delta_{C_{SM}}^l)}{4}, \Delta_{C_{SM}}^l > 0 \text{ and } \Delta_{C_{SM}}^u > 0
\end{aligned}$$

$$d(\widetilde{C}_{TA}, \tilde{0}) = C_{TA} + \frac{(\Delta_{C_{TA}}^u - \Delta_{C_{TA}}^l)}{4}, \Delta_{C_{TA}}^l > 0 \text{ and } \Delta_{C_{TA}}^l > 0$$

$$d(\widetilde{C}_{PA}, \tilde{0}) = C_{PA} + \frac{(\Delta_{C_{PA}}^u - \Delta_{C_{PA}}^l)}{4}, \Delta_{C_{PA}}^l > 0 \text{ and } \Delta_{C_{PA}}^l > 0$$

$$d(\widetilde{C}_{TM_i}, \tilde{0}) = C_{TM_i} + \frac{(\Delta_{C_{TM_i}}^u - \Delta_{C_{TM_i}}^l)}{4}, \Delta_{C_{TM_i}}^l > 0 \text{ and } a_{C_{TM_i}}^l > 0$$

$$d(\widetilde{C}_{OR_i}, \tilde{0}) = C_{OR_i} + \frac{(\Delta_{C_{OR_i}}^u - \Delta_{C_{OR_i}}^l)}{4}, \Delta_{C_{OR_i}}^l > 0 \text{ and } \Delta_{C_{OR_i}}^l > 0$$

$$d(\widetilde{C}_{SR_i}, \tilde{0}) = C_{SR_i} + \frac{(\Delta_{C_{SR_i}}^u - \Delta_{C_{SR_i}}^l)}{4}, \Delta_{C_{SR_i}}^l > 0 \text{ and } \Delta_{C_{SR_i}}^l > 0$$

$$d(\widetilde{C}_{B_i}, \tilde{0}) = C_{B_i} + \frac{(\Delta_{C_{B_i}}^u - \Delta_{C_{B_i}}^l)}{4}, \Delta_{C_{B_i}}^l > 0 \text{ and } \Delta_{C_{B_i}}^l > 0$$

$$d(\widetilde{C}_{L_i}, \tilde{0}) = C_{L_i} + \frac{(\Delta_{C_{L_i}}^u - \Delta_{C_{L_i}}^l)}{4}, \Delta_{C_{L_i}}^l > 0 \text{ and } \Delta_{C_{L_i}}^l > 0$$

$$d(\widetilde{H}_M, \tilde{0}) = H_M + \frac{(\Delta_{H_M}^u - \Delta_{H_M}^l)}{4}, \Delta_{H_M}^l > 0 \text{ and } \Delta_{H_M}^l > 0$$

$$d(\widetilde{H}_{R_i}, \tilde{0}) = H_{R_i} + \frac{(\Delta_{H_{R_i}}^u - \Delta_{H_{R_i}}^l)}{4}, \Delta_{H_{R_i}}^l > 0 \text{ and } \Delta_{H_{R_i}}^l > 0$$

$$d(\widetilde{H}_{WR_i}, \tilde{0}) = H_{WR_i} + \frac{(\Delta_{H_{WR_i}}^u - \Delta_{H_{WR_i}}^l)}{4}, \Delta_{H_{WR_i}}^l > 0 \text{ and } ta_{H_{WR_i}}^l > 0$$

$$d(\widetilde{H}_{DR_i}, \tilde{0}) = H_{DR_i} + \frac{(\Delta_{H_{DR_i}}^u - \Delta_{H_{DR_i}}^l)}{4}, \Delta_{H_{DR_i}}^l > 0 \text{ and } a_{H_{DR_i}}^l > 0$$

$$d(\tilde{\epsilon}, \tilde{0}) = \epsilon + \frac{(\Delta_{\epsilon}^u - \Delta_{\epsilon}^l)}{4}, \Delta_{\epsilon}^l > 0 \text{ and } \Delta_{\epsilon}^l > 0$$



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