

*Research article***Forecasting mixture composition in the extractive distillation of n-hexane and ethyl acetate with n-methyl-2-pyrrolidone through ANN for a preliminary energy assessment****Daniel Chuquin-Vasco^{1,*}, Dennise Chicaiza-Sagal², Cristina Calderón-Tapia³, Nelson Chuquin-Vasco⁴, Juan Chuquin-Vasco⁴ and Lidia Castro-Cepeda⁵**

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Appendix A: Sensitivity analysis

The critical variables affecting the quality of n-hexane and ethyl acetate, the products of interest when modified in the extractive distillation and solvent recovery stages, were selected. Table A1 details the parameters that directly influence the purity of the components of interest.

Table A1. Variables used in the sensitivity analysis.

| ANN | Column | Nomenclature | Parameter | Units |
|---------|------------------|-----------------------|--|-------|
| | | T1-F | Feed flow inlet temperature | °C |
| Inputs | Extractive (EDC) | RR-EDC | EDC tower reflux ratio | |
| | | FM1-F | Feed Stream Mass Flow | kg/h |
| | Recovery (ERC) | FM2-MU | Make-up stream mass flow | kg/h |
| | | T-B1 | Flow inlet temperature to ERC | °C |
| Outputs | Recovery (ERC) | RR-ERC | ERC tower reflux ratio | - |
| | | FM-B1 | Mass flow of the B1 stream (mixture) | kg/h |
| | Extractive (EDC) | X _{HE} -EDC | Mole fraction of n-hexane in the distillate of EDC | - |
| | | X _{NMP} -EDC | Mole fraction of N-methyl-2 pyrrolidone in the bottom of EDC | - |
| | Recovery (ERC) | X _{EA} -ERC | Mole fraction of ethyl acetate in the distillate of ERC | - |
| | | X _{NMP} -ERC | Mole fraction of N-methyl-2 pyrrolidone in the bottom of ERC | - |

A.1. Results of the sensitivity analysis in the extractive distillation column

Four sensitivity analyses were performed on the most relevant design variables in the extractive distillation column (EDC): feed flow temperature, reflux ratio of the extractive distillation column, mass flow of the feed stream, and mass flow of the reflux stream. The parametric study was carried out using the tool available in ChemSep, applying different operating ranges based on the simulation performed in DWSIM. Table A2 details the sensitivity analyses performed in the EDC.

Table A2. Sensitivity analysis in the extractive distillation column.

| Extractive distillation (EDC) | | | |
|-------------------------------|---|----------------------|--------------------------------------|
| # Analyses | Description | Independent variable | Dependent variable |
| 1 | Analysis of the effect of the feed temperature to the EDC | T1-F | X _{HE} X _{NMP1} |
| 2 | Analysis of the effect of the reflux ratio in the EDC | RR-ERC | X _{HE} X _{NMP1} |
| 3 | Analysis of the effect of the mass flow of the feed | FM1-F | X _{HE} X _{NMP1} |
| 4 | Analysis of the effect of the make-up mass flow | FM2-MU | X _{HE} X _{NMP1} |

A.1.1. Results of analysis #1

The ranges established for the analysis on the effect of the feed temperature in the EDC column were 20–150 °C, necessary to avoid overheating the outlet fluid of the recovered solvent in the heat exchanger (Figure A1). This design variable is used as an input for the ANN because there are significant changes in the fractions of n-hexane in the distillate, which decreases from 0.956 to 0.4 (a 58.3% decrease), and the NMP fraction in the bottom decreases from 0.556 to 0.478 (a 14.0% decrease) as the feed temperature increases. In both cases, as the inlet temperature rises, the molar fraction of the components decreases. The feed temperature directly impacts the column behavior, with higher temperatures reducing n-hexane recovery in the distillate and NMP purity at the bottom.

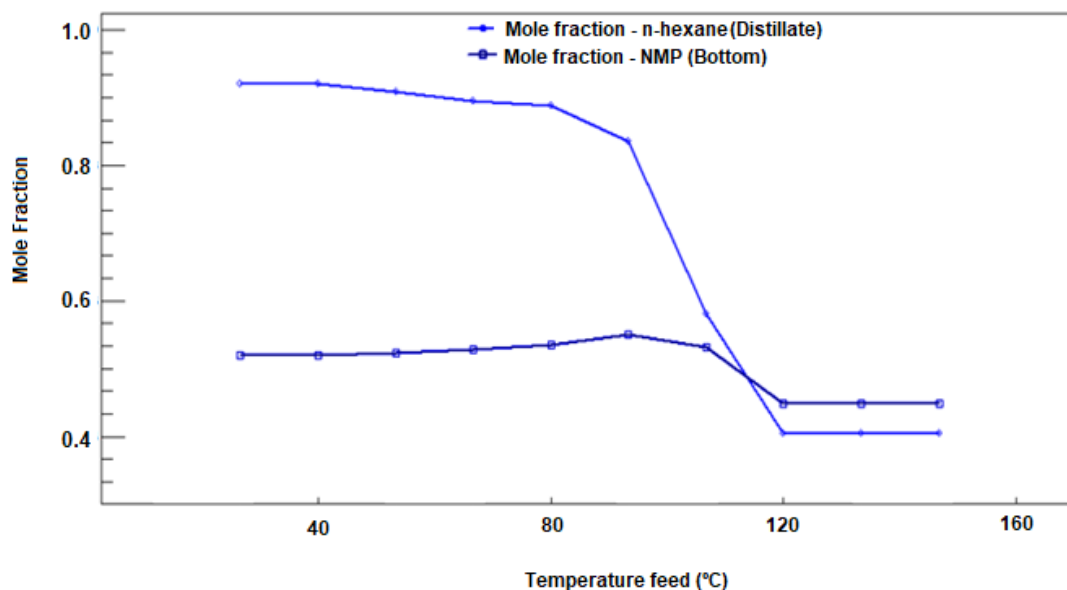


Figure A1. Molar fraction vs feed temperature to EDC.

A.1.2. Results of analysis #2

For the analysis of the reflux ratio of the EDC tower, a range of 0.7 to 2 was used, as observed in Figure A2. There is no significant increase in the fraction of n-hexane in the distillate or NMP in the bottom. The n-hexane practically remains constant with a fraction of 0.92 while the NMP changes from 0.51 to 0.49 (a 3.9% decrease). Therefore, as there are minimal changes in the key component fractions over the reflux ratio range analyzed, this variable is discarded as an input to the ANN model.

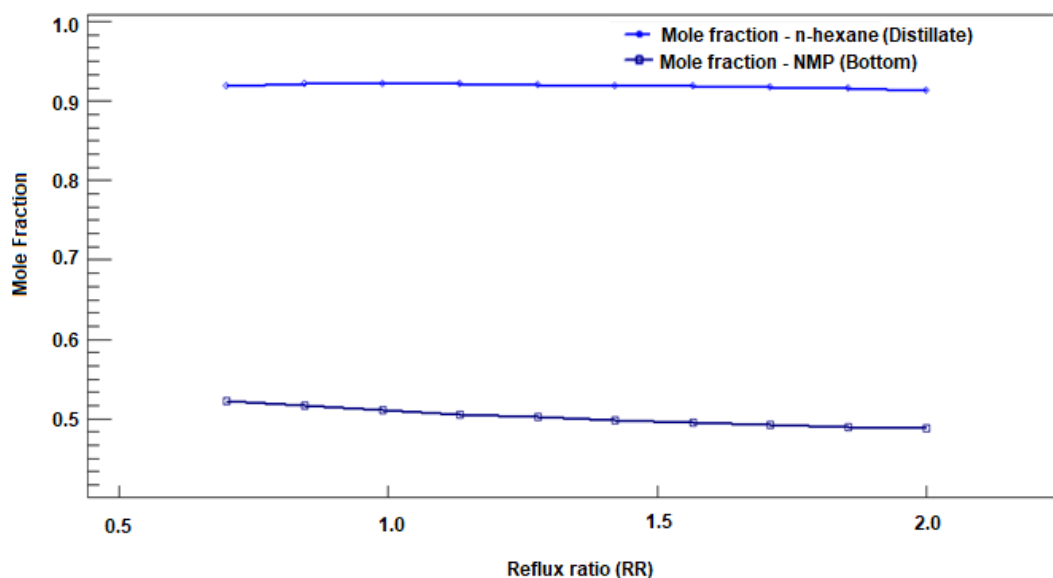


Figure A2. Molar fraction vs EDC reflux ratio.

A.1.3. Results of analysis #3

For this analysis, the mass flow rate of the feed was varied in a range from 8000 to 10,000 kg/h. In Figure A3, a significant increase in the molar fraction of NMP obtained at the bottom is shown, increasing from 0.37 to 0.69 (an 86.5% increase), while in the case of n-hexane, a decrease in its composition in the distillate is observed as the mass feed flow rate increases, with the fraction decreasing from 0.95 to 0.85 (a 10.5% decrease). Since there is a significant change in the concentrations with respect to the mass flow rate of the feed, this variable is taken as an input to the ANN model. The feed flow rate impacts the residence time and partial pressure of components in the column, directly altering the separation efficiency. Correlating this operational parameter will allow the optimization of purity and recovery targets.

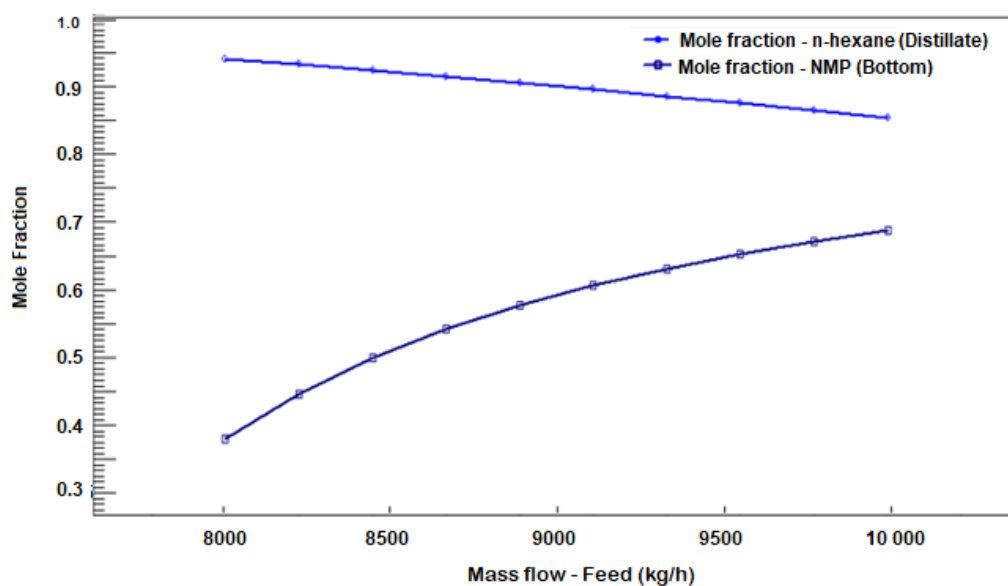


Figure A3. Molar fraction vs Mass flow-Feed.

A.1.4. Results of analysis #4

For this analysis, a range of 3 to 100 kg/h was used for the make-up flow rate entering the EDC. In Figure A4, a significant increase in n-hexane in the distillate is observed, with the molar fraction changing from 0.2 to 0.92 (a 360% increase), while the NMP fraction decreases from 1.0 to 0.3 (a 70% decrease). Since there are these significant changes, the make-up flow rate is chosen as an input to the ANN model. The make-up stream impacts the composition profile in the column, directly altering the recovery and purity. Correlating this operational parameter will allow the optimization of separation efficiency to achieve purity and recovery targets.

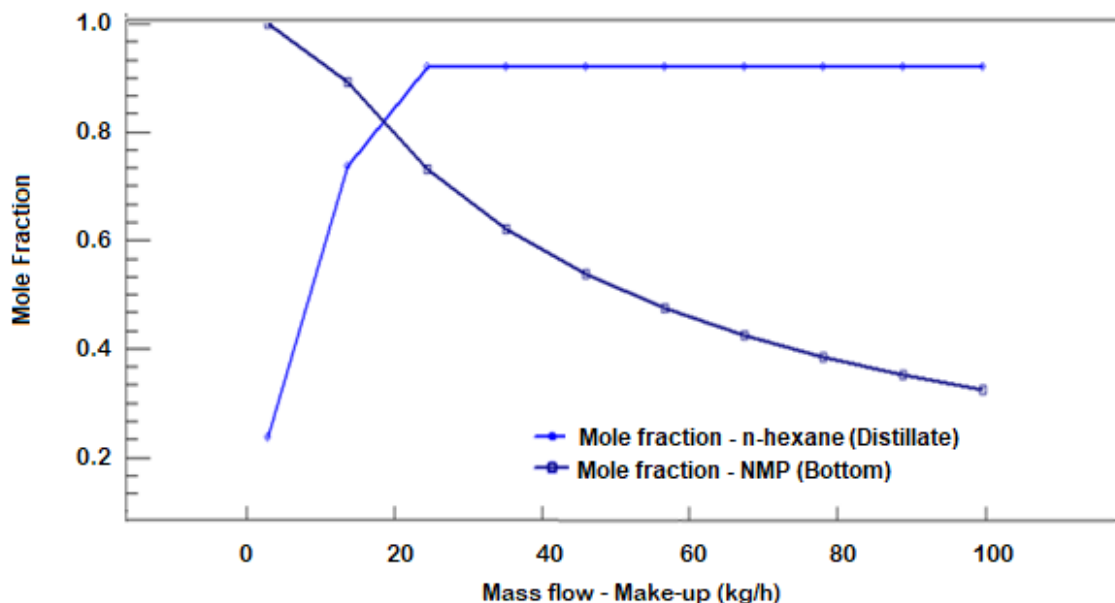


Figure A4. Molar fraction vs Mass flow—Make-up.

A.2. Results of the sensitivity analysis in the recovery distillation column

Three sensitivity analyses were performed on the most relevant design variables in the recovery distillation column (ERC): feed flow temperature, reflux ratio of the recovery column, and mass flow rate of stream B1 (Table A3). The parametric study was carried out using the tool available in ChemSep, applying different operating ranges based on the simulation performed in DWSIM. The key parameters were identified that have the most influence on purity and recovery of solvent and product. Understanding the relationships between inputs and outputs will allow developing an optimized model for the separation system.

Table A3. Sensitivity analysis in the recovery distillation column.

| Recovery distillation (ERC) | | | |
|-----------------------------|---|----------------------|--------------------|
| # Analyses | Description | Independent variable | Dependent variable |
| 5 | Analysis of the effect of B1 feed temperature to the recovery extractive column | T-B1 | X_AE X_NMP2 |
| 6 | Analysis of the effect of the reflux ratio in the ERC | RR-ERC | X_AE X_NMP2 |
| 7 | Analysis of the effect of B1 feed mass flow rate | FM-B1 | X_AE X_NMP2 |

A.2.1. Results of analysis #5

For the analysis of the B1 feed stream temperature to the ERC, a range of 100 to 120 °C was used. The results shown in Figure A5 demonstrate that the molar fraction of ethyl acetate in the ERC distillate and NMP in the ERC bottom remains constant throughout the analysis. Therefore, this parameter is discarded as a design variable for the ANN model since it has minimal effect on the component separations under the conditions evaluated.

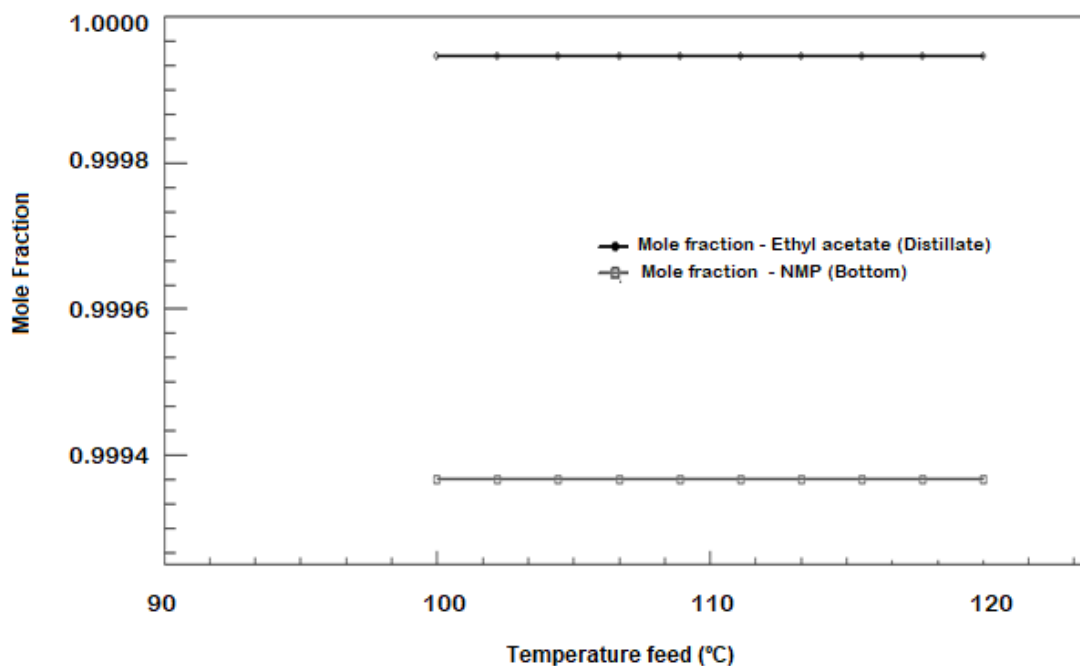


Figure A5. Molar fraction vs feed temperature to ERC.

A.2.2. Results of analysis #6

For the analysis of the reflux ratio in the ERC, a range of 0.8 to 2.0 was employed. Figure A6 illustrates the observed variation in the increase of molar fractions for the targeted components. The molar fraction of Ethyl Acetate in the distillate changes from 0.83 to 1 (a 20% increase), while NMP changes from 0.91 to 0.98 (a 7.69% increase). Consequently, the reflux ratio is selected as the input variable for the development of the ANN.

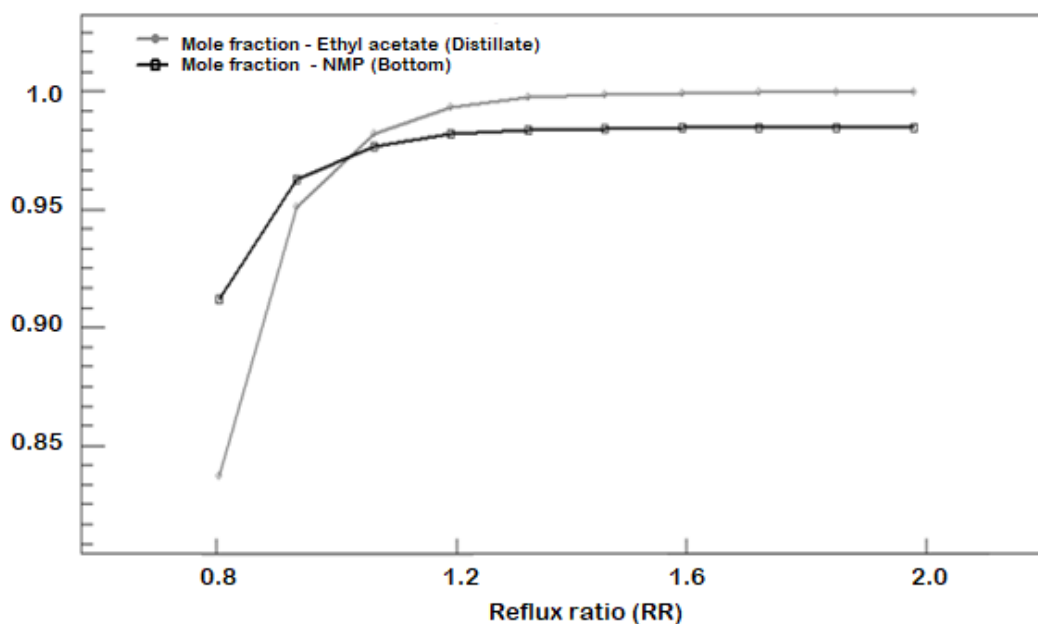


Figure A6. Molar fraction vs ERC reflux ratio.

A.2.3. Results of analysis #7

The feed flow rate to the ERC was ultimately varied within the range of 10,000 to 20,000 kg/h. As depicted in Figure A7, it is evident that the molar fractions of the targeted compounds remain constant across this range. Consequently, this parameter is not chosen as an input for the ANN due to its lack of significant impact on the observed variations in the molar fractions of the compounds of interest.

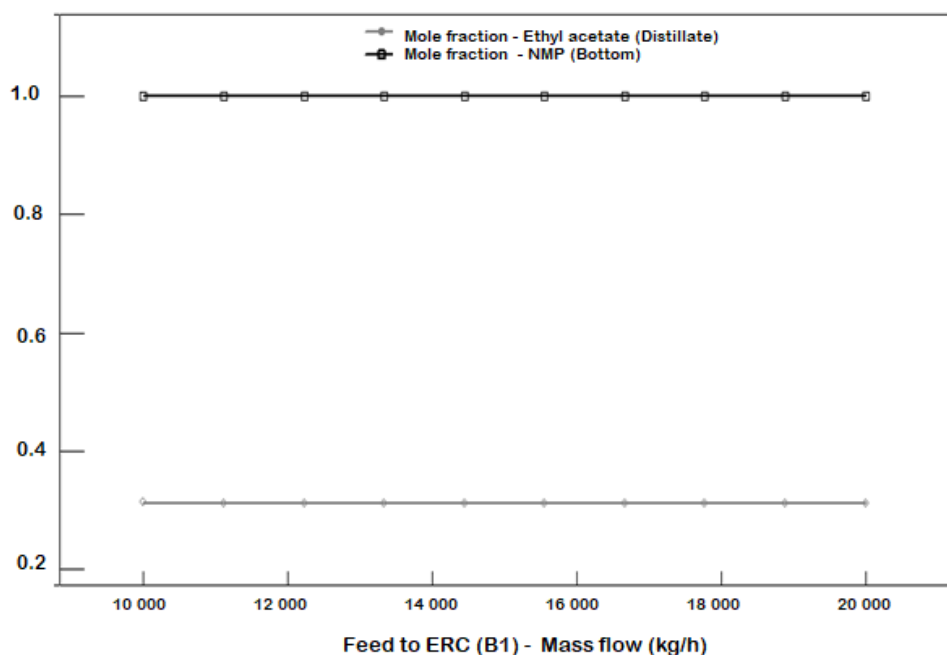


Figure A7. Molar fraction vs Feed mass flow rate to ERC.

Appendix B: Database generated for simulation parameters, training, and validation of the ANN

The database was established by a random number considering restrictions of mass flow, temperature and reflux ratio. Our objective, in addition to simulating and predicting the compositions at the outlet of the Extractive Distillation (EDC) and Recovery Column (ERC).

| Data pair | Inputs | | | | Outputs | | | |
|-----------|------------------------|-------------------------------|-----------------------------------|---------------------------------|-----------------------------|--------------------------|-----------------------------|--------------------------|
| | Feed flow inlet (T1-F) | Feed stream mass flow (FM1-F) | Make-up stream mass flow (FM2-MU) | ERC tower reflux ratio (RR-ERC) | Distillate of EDC (XHE-EDC) | Bottom of EDC (XNMP-EDC) | Distillate of ERC (XEA-ERC) | Bottom of ERC (XNMP-ERC) |
| 1 | 50 | 0.87 | 9706 | 69 | 0.8110 | 0.7576 | 0.9755 | 0.9999 |
| 2 | 78 | 1.2 | 9518 | 67 | 0.9487 | 0.6888 | 0.9830 | 1.0000 |
| 3 | 130 | 1.65 | 8278 | 16 | 0.9960 | 0.6710 | 0.8725 | 1.0000 |
| 4 | 97 | 1.88 | 9158 | 17 | 0.9948 | 0.6187 | 0.7675 | 1.0000 |
| 5 | 107 | 1.1 | 9816 | 29 | 0.9137 | 0.6965 | 0.9923 | 1.0000 |
| 6 | 27 | 0.89 | 9935 | 22 | 1.0000 | 0.4881 | 0.4925 | 1.0000 |
| 7 | 106 | 1.54 | 8409 | 50 | 0.9954 | 0.6792 | 0.9076 | 1.0000 |
| 8 | 49 | 1.38 | 8973 | 83 | 0.9929 | 0.6801 | 0.9567 | 1.0000 |

| | | | | | | | | |
|----|-----|------|------|----|--------|--------|--------|--------|
| 9 | 22 | 1.55 | 9766 | 5 | 1.0000 | 0.4760 | 0.4632 | 1.0000 |
| 10 | 54 | 1.96 | 9022 | 62 | 0.9954 | 0.6183 | 0.7451 | 1.0000 |
| 11 | 40 | 1.9 | 9478 | 73 | 0.9943 | 0.6082 | 0.7470 | 1.0000 |
| 12 | 89 | 1.42 | 8511 | 45 | 0.9944 | 0.6904 | 0.9670 | 1.0000 |
| 13 | 145 | 1.6 | 8344 | 83 | 0.9959 | 0.6757 | 0.8767 | 1.0000 |
| 14 | 22 | 0.9 | 9446 | 54 | 1.0000 | 0.5047 | 0.4967 | 1.0000 |
| 15 | 118 | 1.5 | 8037 | 79 | 0.9961 | 0.6990 | 0.9404 | 1.0000 |
| 16 | 74 | 1.1 | 9023 | 94 | 0.8913 | 0.7260 | 0.9719 | 1.0000 |
| 17 | 107 | 1.8 | 8307 | 89 | 0.9966 | 0.6573 | 0.8043 | 1.0000 |
| 18 | 101 | 0.8 | 8959 | 22 | 0.7623 | 0.7893 | 0.9895 | 0.9781 |
| 19 | 106 | 1.6 | 8690 | 48 | 0.9951 | 0.6621 | 0.8690 | 1.0000 |
| 20 | 116 | 1 | 9240 | 26 | 0.8549 | 0.7387 | 0.9915 | 1.0000 |
| 21 | 75 | 1.5 | 9922 | 69 | 0.9910 | 0.6323 | 0.8612 | 1.0000 |
| 22 | 46 | 1.4 | 9960 | 25 | 0.9896 | 0.6424 | 0.9131 | 1.0000 |
| 23 | 28 | 1.7 | 9025 | 67 | 1.0000 | 0.4986 | 0.4618 | 1.0000 |
| 24 | 101 | 1.5 | 8128 | 9 | 0.9957 | 0.6937 | 0.9525 | 1.0000 |
| 25 | 140 | 1.44 | 8480 | 22 | 0.9945 | 0.6883 | 0.9627 | 1.0000 |
| 26 | 93 | 1.67 | 9715 | 99 | 0.9946 | 0.6214 | 0.8009 | 1.0000 |
| 27 | 27 | 1.72 | 9281 | 62 | 1.0000 | 0.4898 | 0.4591 | 1.0000 |
| 28 | 71 | 1.02 | 9388 | 92 | 0.8676 | 0.7302 | 0.9719 | 1.0000 |
| 29 | 61 | 1.67 | 9781 | 19 | 0.9924 | 0.6171 | 0.8108 | 1.0000 |
| 30 | 88 | 1.59 | 9032 | 18 | 0.9941 | 0.6503 | 0.8652 | 1.0000 |
| 31 | 36 | 1 | 8757 | 75 | 0.8411 | 0.7578 | 0.9734 | 1.0000 |
| 32 | 107 | 1.2 | 9808 | 44 | 0.9570 | 0.6784 | 0.9893 | 1.0000 |
| 33 | 23 | 1.8 | 8876 | 22 | 1.0000 | 0.5005 | 0.4624 | 1.0000 |
| 34 | 41 | 1.6 | 9038 | 59 | 0.9941 | 0.6501 | 0.8535 | 1.0000 |
| 35 | 43 | 2 | 8904 | 41 | 0.9957 | 0.6187 | 0.7417 | 1.0000 |
| 36 | 80 | 0.87 | 8330 | 15 | 0.7741 | 0.7959 | 0.9927 | 0.9839 |
| 37 | 87 | 1.38 | 8244 | 18 | 0.9819 | 0.7055 | 0.9950 | 1.0000 |
| 38 | 44 | 1.9 | 9299 | 50 | 0.9945 | 0.6134 | 0.7543 | 1.0000 |
| 39 | 108 | 0.82 | 9611 | 34 | 0.7871 | 0.7756 | 0.9864 | 0.9995 |
| 40 | 82 | 1.9 | 8089 | 61 | 0.9971 | 0.6561 | 0.7871 | 1.0000 |
| 41 | 32 | 1 | 9948 | 88 | 1.0000 | 0.4860 | 0.4818 | 1.0000 |
| 42 | 50 | 1.3 | 9061 | 78 | 0.9774 | 0.6886 | 0.9803 | 1.0000 |
| 43 | 68 | 1.1 | 8960 | 56 | 0.9774 | 0.7274 | 0.9828 | 1.0000 |
| 44 | 63 | 1.52 | 8205 | 71 | 0.9958 | 0.6898 | 0.9229 | 1.0000 |
| 45 | 81 | 0.92 | 9602 | 73 | 0.8301 | 0.7472 | 0.9755 | 1.0000 |
| 46 | 35 | 1.18 | 8905 | 69 | 0.9215 | 0.7142 | 0.9803 | 1.0000 |
| 47 | 59 | 1.48 | 8005 | 61 | 0.9960 | 0.7023 | 0.9578 | 1.0000 |
| 48 | 98 | 1.09 | 8044 | 7 | 0.8554 | 0.7639 | 0.9974 | 1.0000 |
| 49 | 76 | 0.8 | 8940 | 29 | 0.7618 | 0.7900 | 0.9861 | 0.9779 |
| 50 | 65 | 1.9 | 9884 | 43 | 0.9938 | 0.5945 | 0.7417 | 1.0000 |
| 51 | 107 | 0.9 | 9205 | 57 | 0.8113 | 0.7668 | 0.9786 | 0.9999 |
| 52 | 102 | 1.2 | 8686 | 96 | 0.9228 | 0.7193 | 0.9722 | 1.0000 |
| 53 | 124 | 1.5 | 8624 | 18 | 0.9946 | 0.6753 | 0.9237 | 1.0000 |
| 54 | 148 | 2 | 8047 | 5 | 0.9972 | 0.6484 | 0.7713 | 1.0000 |

| | | | | | | | | |
|-----|-----|------|------|----|--------|--------|--------|--------|
| 55 | 63 | 1.9 | 8373 | 61 | 0.9966 | 0.6456 | 0.7780 | 1.0000 |
| 56 | 103 | 1.8 | 9783 | 88 | 0.9931 | 0.6071 | 0.7630 | 1.0000 |
| 57 | 20 | 1.3 | 9852 | 69 | 1.0000 | 0.4804 | 0.4687 | 1.0000 |
| 58 | 53 | 1.6 | 9820 | 96 | 0.9923 | 0.6251 | 0.8219 | 1.0000 |
| 59 | 128 | 2 | 8910 | 48 | 0.9957 | 0.6187 | 0.7406 | 1.0000 |
| 60 | 36 | 1.5 | 9175 | 96 | 0.9933 | 0.6577 | 0.8836 | 1.0000 |
| 61 | 24 | 1.9 | 8398 | 95 | 1.0000 | 0.5174 | 0.4599 | 1.0000 |
| 62 | 77 | 0.9 | 8059 | 50 | 0.7781 | 0.8019 | 0.9749 | 0.9877 |
| 63 | 89 | 1.3 | 8292 | 13 | 0.9507 | 0.7155 | 0.9964 | 1.0000 |
| 64 | 23 | 1.5 | 9267 | 83 | 1.0000 | 0.4950 | 0.4656 | 1.0000 |
| 65 | 39 | 1.71 | 8262 | 50 | 0.9963 | 0.6664 | 0.8433 | 1.0000 |
| 66 | 93 | 1.84 | 8068 | 46 | 0.9970 | 0.6616 | 0.8080 | 1.0000 |
| 67 | 35 | 0.96 | 8507 | 55 | 0.8168 | 0.7771 | 0.9781 | 0.9999 |
| 68 | 113 | 1.6 | 9742 | 13 | 0.9920 | 0.6254 | 0.8371 | 1.0000 |
| 69 | 55 | 1.62 | 9049 | 29 | 0.9942 | 0.6468 | 0.8507 | 1.0000 |
| 70 | 84 | 0.9 | 8429 | 16 | 0.7895 | 0.7943 | 0.9928 | 0.9978 |
| 71 | 22 | 1.5 | 8677 | 19 | 1.0000 | 0.5131 | 0.4756 | 1.0000 |
| 72 | 130 | 1.2 | 8905 | 79 | 0.9300 | 0.7108 | 0.9779 | 1.0000 |
| 73 | 77 | 1.1 | 8448 | 94 | 0.8732 | 0.7477 | 0.9687 | 1.0000 |
| 74 | 107 | 1.3 | 8424 | 34 | 0.9555 | 0.7110 | 0.9903 | 1.0000 |
| 75 | 50 | 0.8 | 9819 | 57 | 0.7833 | 0.7753 | 0.9775 | 0.9995 |
| 76 | 68 | 1.78 | 8768 | 58 | 0.9955 | 0.6417 | 0.8006 | 1.0000 |
| 77 | 95 | 1.88 | 9769 | 55 | 0.9934 | 0.6000 | 0.7475 | 1.0000 |
| 78 | 102 | 1.29 | 9698 | 24 | 0.9886 | 0.6668 | 0.9876 | 1.0000 |
| 79 | 87 | 1.62 | 9393 | 89 | 0.9935 | 0.6367 | 0.8289 | 1.0000 |
| 80 | 31 | 1.71 | 8308 | 75 | 0.9963 | 0.6654 | 0.8368 | 1.0000 |
| 81 | 55 | 0.9 | 8711 | 18 | 0.7977 | 0.7845 | 0.9924 | 0.9995 |
| 82 | 64 | 1.22 | 9587 | 67 | 0.9594 | 0.6830 | 0.9835 | 1.0000 |
| 83 | 109 | 1.18 | 8615 | 88 | 0.9121 | 0.7255 | 0.9737 | 1.0000 |
| 84 | 99 | 1.26 | 9734 | 37 | 0.9810 | 0.6706 | 0.9912 | 1.0000 |
| 85 | 98 | 0.87 | 9857 | 38 | 0.8146 | 0.7516 | 0.9867 | 0.9999 |
| 86 | 81 | 0.86 | 9763 | 86 | 0.8146 | 0.7590 | 0.9694 | 0.9999 |
| 87 | 69 | 1.43 | 9402 | 91 | 0.9921 | 0.6586 | 0.9085 | 1.0000 |
| 88 | 109 | 2 | 9146 | 80 | 0.9953 | 0.6117 | 0.7309 | 1.0000 |
| 89 | 81 | 1.4 | 9746 | 16 | 0.9898 | 0.6491 | 0.9237 | 1.0000 |
| 90 | 141 | 1.8 | 8921 | 17 | 0.9951 | 0.6335 | 0.7964 | 1.0000 |
| 91 | 28 | 1.9 | 8341 | 14 | 1.0000 | 0.5171 | 0.4652 | 1.0000 |
| 92 | 114 | 0.8 | 9999 | 52 | 0.7873 | 0.7690 | 0.9802 | 0.9997 |
| 93 | 60 | 1.21 | 9604 | 14 | 0.9555 | 0.6828 | 0.9965 | 1.0000 |
| 94 | 22 | 1.58 | 8500 | 32 | 1.0000 | 0.5180 | 0.4736 | 1.0000 |
| 95 | 54 | 0.99 | 8780 | 69 | 0.8375 | 0.7592 | 0.9753 | 1.0000 |
| 96 | 80 | 1.5 | 9151 | 85 | 0.9934 | 0.6583 | 0.8866 | 1.0000 |
| 97 | 116 | 0.84 | 9249 | 42 | 0.7868 | 0.7825 | 0.9826 | 0.9993 |
| 98 | 65 | 0.93 | 8886 | 43 | 0.8153 | 0.7701 | 0.9834 | 0.9999 |
| 99 | 90 | 1.4 | 8513 | 40 | 0.9943 | 0.6930 | 0.9801 | 1.0000 |
| 100 | 90 | 1 | 8765 | 47 | 0.8413 | 0.7569 | 0.9832 | 1.0000 |

| | | | | | | | | |
|-----|-----|------|------|----|--------|--------|--------|--------|
| 101 | 30 | 1.3 | 8532 | 46 | 0.9594 | 0.7072 | 0.9872 | 1.0000 |
| 102 | 120 | 1.7 | 8547 | 6 | 0.9956 | 0.6558 | 0.8440 | 1.0000 |
| 103 | 104 | 1.3 | 9088 | 40 | 0.9783 | 0.6867 | 0.9899 | 1.0000 |
| 104 | 55 | 1.4 | 8772 | 86 | 0.9920 | 0.6846 | 0.9547 | 1.0000 |
| 105 | 95 | 0.87 | 9456 | 96 | 0.8049 | 0.7672 | 0.9645 | 0.9999 |
| 106 | 120 | 1.38 | 8171 | 11 | 0.9791 | 0.7081 | 0.9969 | 1.0000 |
| 107 | 85 | 1.66 | 9132 | 79 | 0.9944 | 0.6411 | 0.8247 | 1.0000 |
| 108 | 60 | 1.93 | 9546 | 27 | 0.9940 | 0.6024 | 0.7443 | 1.0000 |
| 109 | 50 | 1.84 | 8973 | 9 | 0.9951 | 0.6280 | 0.7845 | 1.0000 |
| 110 | 61 | 0.81 | 9832 | 44 | 0.7879 | 0.7713 | 0.9829 | 0.9996 |
| 111 | 106 | 1.29 | 8266 | 73 | 0.9456 | 0.7195 | 0.9787 | 1.0000 |
| 112 | 110 | 1.66 | 9363 | 62 | 0.9937 | 0.6329 | 0.8201 | 1.0000 |
| 113 | 68 | 1.24 | 9850 | 48 | 0.9756 | 0.6703 | 0.9887 | 1.0000 |
| 114 | 109 | 0.82 | 9301 | 51 | 0.7795 | 0.7866 | 0.9785 | 0.9985 |
| 115 | 85 | 1.82 | 9606 | 88 | 0.9921 | 0.6110 | 0.7619 | 1.0000 |
| 116 | 31 | 0.94 | 8798 | 55 | 0.8170 | 0.7710 | 0.9788 | 0.9999 |
| 117 | 46 | 1.02 | 8662 | 84 | 0.8466 | 0.7569 | 0.9705 | 1.0000 |
| 118 | 20 | 1.43 | 9361 | 73 | 0.9999 | 0.4931 | 0.4680 | 1.0000 |
| 119 | 102 | 1.24 | 8798 | 41 | 0.9434 | 0.7069 | 0.9886 | 1.0000 |
| 120 | 100 | 0.97 | 8919 | 86 | 0.8332 | 0.7593 | 0.9694 | 1.0000 |
| 121 | 150 | 1.09 | 9138 | 49 | 0.8904 | 0.7228 | 0.9853 | 1.0000 |
| 122 | 28 | 1.73 | 9541 | 40 | 1.0000 | 0.4808 | 0.4576 | 1.0000 |
| 123 | 139 | 0.99 | 8243 | 18 | 0.8210 | 0.7792 | 0.9926 | 0.9999 |
| 124 | 62 | 1.86 | 8264 | 14 | 0.9964 | 0.6517 | 0.8007 | 1.0000 |
| 125 | 116 | 1.3 | 9361 | 95 | 0.9870 | 0.6785 | 0.9772 | 1.0000 |
| 126 | 50 | 0.8 | 9300 | 23 | 0.7709 | 0.7884 | 0.9894 | 0.9928 |
| 127 | 100 | 1.4 | 8060 | 79 | 0.9829 | 0.7112 | 0.9779 | 1.0000 |
| 128 | 43 | 1.9 | 9954 | 80 | 0.9931 | 0.5934 | 0.7358 | 1.0000 |
| 129 | 92 | 1.8 | 9457 | 7 | 0.9931 | 0.6153 | 0.7823 | 1.0000 |
| 130 | 96 | 0.86 | 8560 | 9 | 0.7766 | 0.7940 | 0.9960 | 0.9892 |
| 131 | 39 | 1.61 | 9944 | 46 | 0.9861 | 0.6188 | 0.8223 | 1.0000 |
| 132 | 86 | 1.08 | 8740 | 57 | 0.8742 | 0.7399 | 0.9814 | 1.0000 |
| 133 | 115 | 1.82 | 9776 | 92 | 0.9933 | 0.6057 | 0.7574 | 1.0000 |
| 134 | 40 | 1.07 | 8490 | 27 | 0.8621 | 0.7509 | 0.9906 | 1.0000 |
| 135 | 110 | 1.77 | 9946 | 89 | 0.9927 | 0.6046 | 0.7671 | 1.0000 |
| 136 | 139 | 1.42 | 8197 | 60 | 0.9927 | 0.7027 | 0.9817 | 1.0000 |
| 137 | 104 | 1.13 | 9928 | 48 | 0.9298 | 0.6873 | 0.9878 | 1.0000 |
| 138 | 93 | 1.44 | 8631 | 23 | 0.9942 | 0.6828 | 0.9541 | 1.0000 |
| 139 | 73 | 0.93 | 9976 | 22 | 0.8436 | 0.7303 | 0.9931 | 1.0000 |
| 140 | 108 | 1.52 | 9010 | 74 | 0.9939 | 0.6605 | 0.8853 | 1.0000 |
| 141 | 23 | 1.64 | 8049 | 97 | 1.0000 | 0.5352 | 0.4728 | 1.0000 |
| 142 | 136 | 1.07 | 8577 | 31 | 0.8649 | 0.7477 | 0.9894 | 1.0000 |
| 143 | 50 | 1.17 | 8077 | 43 | 0.8893 | 0.7473 | 0.9854 | 1.0000 |
| 144 | 36 | 1.13 | 9131 | 16 | 0.9073 | 0.7142 | 0.9953 | 1.0000 |
| 145 | 101 | 1.29 | 8277 | 90 | 0.9460 | 0.7195 | 0.9739 | 1.0000 |
| 146 | 89 | 1.58 | 9095 | 83 | 0.9941 | 0.6509 | 0.8551 | 1.0000 |

| | | | | | | | | |
|-----|-----|------|------|----|--------|--------|--------|--------|
| 147 | 138 | 1.4 | 8718 | 89 | 0.9939 | 0.6866 | 0.9569 | 1.0000 |
| 148 | 46 | 1.56 | 8567 | 75 | 0.9953 | 0.6717 | 0.8859 | 1.0000 |
| 149 | 108 | 1.05 | 9292 | 27 | 0.8778 | 0.7253 | 0.9917 | 1.0000 |
| 150 | 107 | 0.84 | 9912 | 52 | 0.8028 | 0.7592 | 0.9812 | 0.9999 |
| 151 | 57 | 1.1 | 8358 | 69 | 0.8702 | 0.7506 | 0.9764 | 1.0000 |
| 152 | 67 | 1.14 | 9459 | 55 | 0.9212 | 0.7015 | 0.9851 | 1.0000 |
| 153 | 26 | 0.9 | 8054 | 38 | 1.0000 | 0.5563 | 0.5226 | 1.0000 |
| 154 | 66 | 1.5 | 9176 | 31 | 0.9932 | 0.6560 | 0.8959 | 1.0000 |
| 155 | 42 | 1.3 | 8903 | 93 | 0.9722 | 0.6946 | 0.9760 | 1.0000 |
| 156 | 108 | 1.2 | 9891 | 19 | 0.9593 | 0.6750 | 0.9954 | 1.0000 |
| 157 | 49 | 1.3 | 8506 | 58 | 0.9584 | 0.7084 | 0.9838 | 1.0000 |
| 158 | 22 | 0.81 | 9042 | 57 | 1.0000 | 0.5226 | 0.5102 | 1.0000 |
| 159 | 42 | 1.13 | 9427 | 9 | 0.9160 | 0.7035 | 0.9975 | 1.0000 |
| 160 | 45 | 0.89 | 8652 | 45 | 0.7918 | 0.7900 | 0.9805 | 0.9992 |
| 161 | 109 | 0.85 | 9336 | 92 | 0.7933 | 0.7774 | 0.9640 | 0.9997 |
| 162 | 89 | 1.25 | 8009 | 66 | 0.9195 | 0.7361 | 0.9790 | 1.0000 |
| 163 | 62 | 1.82 | 8184 | 86 | 0.9968 | 0.6600 | 0.8029 | 1.0000 |
| 164 | 135 | 0.92 | 8403 | 89 | 0.7970 | 0.7924 | 0.9619 | 0.9995 |
| 165 | 91 | 1.69 | 8742 | 49 | 0.9948 | 0.6509 | 0.8326 | 1.0000 |
| 166 | 135 | 1.92 | 8998 | 42 | 0.9953 | 0.6216 | 0.7580 | 1.0000 |
| 167 | 42 | 1.77 | 8215 | 48 | 0.9966 | 0.6624 | 0.8246 | 1.0000 |
| 168 | 71 | 1.59 | 8388 | 63 | 0.9957 | 0.6746 | 0.8831 | 1.0000 |
| 169 | 50 | 0.9 | 9081 | 63 | 0.8080 | 0.7715 | 0.9758 | 0.9999 |
| 170 | 24 | 1 | 9853 | 95 | 0.9998 | 0.4892 | 0.4825 | 1.0000 |
| 171 | 117 | 1.9 | 9373 | 21 | 0.9944 | 0.6101 | 0.7563 | 1.0000 |
| 172 | 22 | 1.2 | 8391 | 53 | 1.0000 | 0.5323 | 0.4925 | 1.0000 |
| 173 | 98 | 1.7 | 8421 | 88 | 0.9961 | 0.6625 | 0.8337 | 1.0000 |
| 174 | 112 | 2 | 9636 | 16 | 0.9939 | 0.5941 | 0.7282 | 1.0000 |
| 175 | 30 | 1.2 | 8818 | 3 | 1.0000 | 0.5152 | 0.4894 | 1.0000 |
| 176 | 75 | 1.69 | 9697 | 21 | 0.9928 | 0.6179 | 0.8065 | 1.0000 |
| 177 | 103 | 1.43 | 9200 | 61 | 0.9925 | 0.6648 | 0.9231 | 1.0000 |
| 178 | 108 | 1.87 | 9864 | 33 | 0.9932 | 0.5972 | 0.7505 | 1.0000 |
| 179 | 101 | 1.29 | 8458 | 30 | 0.9526 | 0.7112 | 0.9914 | 1.0000 |
| 180 | 83 | 0.9 | 8302 | 33 | 0.7856 | 0.7982 | 0.9846 | 0.9960 |
| 181 | 54 | 1.18 | 9689 | 58 | 0.9450 | 0.6863 | 0.9854 | 1.0000 |
| 182 | 34 | 1.81 | 8422 | 76 | 0.9964 | 0.6519 | 0.7997 | 1.0000 |
| 183 | 22 | 0.82 | 8451 | 21 | 1.0000 | 0.5435 | 0.4741 | 1.0000 |
| 184 | 113 | 1.99 | 8459 | 22 | 0.9965 | 0.6345 | 0.7586 | 1.0000 |
| 185 | 96 | 1.19 | 9477 | 41 | 0.9432 | 0.6913 | 0.9894 | 1.0000 |
| 186 | 97 | 1.8 | 9233 | 4 | 0.9943 | 0.6226 | 0.7890 | 1.0000 |
| 187 | 109 | 1.3 | 8336 | 51 | 0.9523 | 0.7147 | 0.9853 | 1.0000 |
| 188 | 35 | 1.53 | 9769 | 12 | 0.9915 | 0.6322 | 0.8635 | 1.0000 |
| 189 | 30 | 0.8 | 9167 | 57 | 0.9999 | 0.5185 | 0.5089 | 1.0000 |
| 190 | 50 | 1.92 | 9692 | 58 | 0.9938 | 0.5994 | 0.7394 | 1.0000 |
| 191 | 132 | 1.69 | 8867 | 61 | 1.0000 | 0.6468 | 0.8261 | 1.0000 |
| 192 | 64 | 1.78 | 9178 | 85 | 0.9951 | 0.6284 | 0.7843 | 1.0000 |

| | | | | | | | | |
|-----|-----|------|------|-----|--------|--------|--------|--------|
| 193 | 108 | 0.99 | 9673 | 19 | 0.8622 | 0.7255 | 0.9942 | 1.0000 |
| 194 | 40 | 1.87 | 9909 | 62 | 0.9928 | 0.5966 | 0.7459 | 1.0000 |
| 195 | 52 | 1.19 | 9625 | 17 | 0.9475 | 0.6856 | 0.9957 | 1.0000 |
| 196 | 43 | 0.84 | 8596 | 45 | 0.7693 | 0.7958 | 0.9784 | 0.9845 |
| 197 | 46 | 1.25 | 9735 | 16 | 0.9767 | 0.6717 | 0.9962 | 1.0000 |
| 198 | 29 | 1.02 | 9681 | 9 | 0.8754 | 0.7179 | 0.9973 | 1.0000 |
| 199 | 106 | 1.32 | 8651 | 98 | 0.9719 | 0.7009 | 0.9740 | 1.0000 |
| 200 | 47 | 1.75 | 8009 | 76 | 0.9969 | 0.6728 | 0.8342 | 1.0000 |
| 201 | 71 | 1.28 | 9523 | 75 | 0.9834 | 0.6755 | 0.9821 | 1.0000 |
| 202 | 33 | 1.95 | 9192 | 94 | 0.9952 | 0.6142 | 0.7391 | 1.0000 |
| 203 | 34 | 0.97 | 8012 | 89 | 0.8052 | 0.7949 | 0.9614 | 0.9996 |
| 204 | 26 | 1.68 | 8722 | 61 | 1.0000 | 0.5090 | 0.4658 | 1.0000 |
| 205 | 32 | 0.84 | 9399 | 95 | 1.0000 | 0.5098 | 0.4995 | 1.0000 |
| 206 | 95 | 1.99 | 9400 | 63 | 0.9947 | 0.6036 | 0.7296 | 1.0000 |
| 207 | 38 | 1.74 | 9292 | 81 | 0.9943 | 0.6281 | 0.7936 | 1.0000 |
| 208 | 79 | 1.57 | 8247 | 76 | 0.9960 | 0.6825 | 0.8957 | 1.0000 |
| 209 | 55 | 1.31 | 9935 | 14 | 0.9881 | 0.6556 | 0.9656 | 1.0000 |
| 210 | 110 | 1.32 | 9325 | 19 | 0.9906 | 0.6748 | 0.9894 | 1.0000 |
| 211 | 28 | 1.07 | 9639 | 58 | 1.0000 | 0.4928 | 0.4829 | 1.0000 |
| 212 | 65 | 0.99 | 9723 | 92 | 0.8635 | 0.7255 | 0.9725 | 1.0000 |
| 213 | 24 | 1.63 | 9092 | 22 | 1.0000 | 0.4964 | 0.4659 | 1.0000 |
| 214 | 97 | 1.89 | 8812 | 30 | 0.9956 | 0.6300 | 0.7725 | 1.0000 |
| 215 | 116 | 1.73 | 9152 | 95 | 0.9946 | 0.6341 | 0.7985 | 1.0000 |
| 216 | 135 | 1.48 | 8560 | 84 | 0.9949 | 0.6818 | 0.9224 | 1.0000 |
| 217 | 69 | 1.07 | 8339 | 49 | 0.8572 | 0.7573 | 0.9825 | 1.0000 |
| 218 | 89 | 0.92 | 8439 | 25 | 0.7981 | 0.7895 | 0.9891 | 0.9993 |
| 219 | 92 | 1.65 | 9303 | 79 | 0.9932 | 0.6364 | 0.8227 | 1.0000 |
| 220 | 27 | 1.3 | 9200 | 100 | 1.0000 | 0.5022 | 0.4738 | 1.0000 |
| 221 | 53 | 1.5 | 8593 | 95 | 0.9950 | 0.6784 | 0.9085 | 1.0000 |
| 222 | 103 | 1.2 | 8405 | 30 | 0.9133 | 0.7285 | 0.9907 | 1.0000 |
| 223 | 57 | 1.9 | 8570 | 36 | 0.9962 | 0.6379 | 0.7760 | 1.0000 |
| 224 | 119 | 1.81 | 8970 | 45 | 0.9946 | 0.6317 | 0.7876 | 1.0000 |
| 225 | 45 | 1.18 | 8927 | 100 | 0.9222 | 0.7141 | 0.9718 | 1.0000 |
| 226 | 45 | 1.73 | 9400 | 54 | 0.9939 | 0.6247 | 0.7976 | 1.0000 |
| 227 | 114 | 1.47 | 9919 | 98 | 0.9909 | 0.6368 | 0.8693 | 1.0000 |
| 228 | 55 | 2 | 8778 | 34 | 0.9959 | 0.6228 | 0.7459 | 1.0000 |
| 229 | 134 | 1.45 | 8748 | 17 | 0.9939 | 0.6770 | 0.9437 | 1.0000 |
| 230 | 27 | 1.1 | 9181 | 74 | 1.0000 | 0.5076 | 0.4860 | 1.0000 |
| 231 | 56 | 1.36 | 9467 | 33 | 0.9908 | 0.6644 | 0.9547 | 1.0000 |
| 232 | 55 | 1.73 | 9006 | 40 | 0.9948 | 0.6376 | 0.8117 | 1.0000 |
| 233 | 124 | 1.17 | 8190 | 95 | 0.8933 | 0.7439 | 0.9689 | 1.0000 |
| 234 | 94 | 1.13 | 8623 | 61 | 0.8914 | 0.7341 | 0.9807 | 1.0000 |
| 235 | 77 | 1.48 | 8280 | 19 | 0.9953 | 0.6906 | 0.9522 | 1.0000 |
| 236 | 36 | 0.89 | 9618 | 83 | 0.8175 | 0.7552 | 0.9711 | 0.9999 |
| 237 | 67 | 1.35 | 8256 | 60 | 0.9700 | 0.7104 | 0.9831 | 1.0000 |
| 238 | 115 | 1.43 | 9236 | 24 | 0.9924 | 0.6625 | 0.9291 | 1.0000 |

| | | | | | | | | |
|-----|-----|------|------|----|--------|--------|--------|--------|
| 239 | 76 | 1.34 | 9511 | 84 | 0.9907 | 0.6671 | 0.9535 | 1.0000 |
| 240 | 60 | 1.05 | 8436 | 27 | 0.8520 | 0.7575 | 0.9902 | 1.0000 |
| 241 | 80 | 1.83 | 8192 | 29 | 0.9967 | 0.6574 | 0.8096 | 1.0000 |
| 242 | 47 | 1.72 | 8021 | 44 | 0.9968 | 0.6744 | 0.8508 | 1.0000 |
| 243 | 108 | 1.92 | 9046 | 6 | 0.9951 | 0.6190 | 0.7619 | 1.0000 |
| 244 | 28 | 1.32 | 9531 | 88 | 1.0000 | 0.4905 | 0.4701 | 1.0000 |
| 245 | 94 | 1.72 | 9692 | 10 | 0.9929 | 0.6149 | 0.7988 | 1.0000 |
| 246 | 70 | 0.93 | 8305 | 16 | 0.7981 | 0.7918 | 0.9929 | 0.9991 |
| 247 | 48 | 0.81 | 9169 | 42 | 0.7719 | 0.7909 | 0.9813 | 0.9938 |
| 248 | 150 | 1.61 | 8969 | 42 | 0.9930 | 0.6510 | 0.8552 | 1.0000 |
| 249 | 107 | 1.99 | 8577 | 29 | 0.9963 | 0.6305 | 0.7543 | 1.0000 |
| 250 | 118 | 1.82 | 8928 | 89 | 0.9954 | 0.6335 | 0.7793 | 1.0000 |



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